

# Finance and Development: A Tale of Two Sectors

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## Abstract

Income differences across countries primarily reflect differences in total factor productivity (TFP). More disaggregate data show that the TFP gap between rich and poor countries varies systematically across industrial sectors of the economy. For example, poor countries are particularly unproductive in manufacturing. We develop a quantitative framework to explain the relationship between aggregate/sector-level TFP and financial development across countries. Financial frictions distort the allocation of capital and talent across production units, adversely affecting measured productivity. In our model, sectors with larger scales of operation (e.g. manufacturing) have more financing needs, and are hence disproportionately vulnerable to financial frictions. Our quantitative analysis shows that financial frictions account for a large part of the observed cross-country differences in output per worker, aggregate TFP, sector-level relative productivity, and capital to output ratios.

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# 1 Introduction

Income per capita differences across countries are primarily accounted for by low total factor productivity (TFP) in poor countries (Klenow and Rodríguez-Clare, 1997; Hall and Jones, 1999). More disaggregate data show that the TFP gap between rich and poor countries varies systematically across industrial sectors of the economy. For instance, poor countries are particularly unproductive in producing manufactured goods, including equipment investment (Hsieh and Klenow, 2007).<sup>1</sup> Here we attempt to explain these facts by building and using a quantitative model of financial markets and economic development.

There are stark differences in financial development across countries, and a large body of empirical and theoretical work has stressed the role of financial markets in economic development. Our model is intended to capture and quantify this role. We discover that, quantitatively, financial frictions explain a large fraction of the cross-country differences in aggregate TFP and sector-level relative productivity.

In our model, financial frictions distort the allocation of capital across heterogeneous establishments and also their entry/exit decisions, lowering aggregate and sector-level TFP as a consequence. Furthermore, the impacts of financial frictions are not equal across sectors. Consistent with the data, sectors that are particularly unproductive in poor countries (e.g. manufacturing) tend to have larger establishments on average than other sectors (e.g. services). Larger scales imply larger financing needs, and the manufacturing sector is disproportionately more vulnerable to financial frictions. Our model replicates the lower productivity of manufacturing relative to services in countries with underdeveloped financial markets.

We build an economy with two sectors (manufacturing and services) that differ in the per-period fixed costs of operating an establishment. This difference in fixed costs leads to a difference in the scale of establishments in the two sectors. In the model, individuals choose in each period whether to operate an establishment in either sector (entrepreneurship) or to supply labor for a wage. Individuals have different levels of entrepreneurial productivity and wealth, with the latter being endogenously determined by forward-looking saving decisions. The entrepreneurial productivity evolves stochastically, generating the need to reallocate capital and labor from previously-productive entrepreneurs to currently-productive ones. Financial frictions hinder this reallocation process.

We model financial frictions in the form of collateral constraints founded on imperfect enforceability of contracts. In an economy with perfect credit markets, occupational choices are based only on comparative advantage: high-productivity individuals become entrepreneurs,

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<sup>1</sup>Jones (1994), Eaton and Kortum (2001), and Herrendorf and Valentinyi (2006) are recent contributions. Also, Balassa (1964) and Samuelson (1964) are the classic citations for tradables vs. non-tradables, which are closely related to the manufacturing vs. services distinction.

and the allocation of capital equalizes marginal products of capital across establishments. With financial frictions in the form of collateral constraints, individuals' occupational choices and entrepreneurs' production decisions are constrained by their available wealth (collateral), even though individuals do partly overcome the constraints over time with self-financing.

We use our model to quantitatively analyze the cross-country patterns in aggregate and sector-level TFP. We discipline our analysis by requiring that a benchmark model with well-functioning financial markets matches the US data on the establishment size distribution across and within sectors (e.g., average scales and thick right-tails of broadly-defined sectors), the dynamics of establishments, and income concentration. We then quantify the relationship between financial development (measured by the ratio of external financing to GDP) and economic development (output per worker, aggregate/sector-level TFP, and capital to output ratios), both in the cross-country data and in the model simulations. Finally, we use detailed data on the establishment size distribution in Mexico and the US to test additional implications of our model.

We find that financial frictions have sizable effects on output per worker, aggregate and sector-level TFP, and capital to output ratios.

The variation in financial development can explain a factor-of-two difference in output per worker across economies, or almost 80 per cent of the difference in output per worker between a country like Mexico and the US. One thing to note is that the agricultural sector is not modeled or analyzed here. This factor-of-two difference goes a long way in explaining the factor-of-five difference in non-agricultural output per worker between the richest and the poorest fifth percentiles of countries. Consistent with the consensus view in the literature, most of the output per worker differences in our model are accounted for by the low TFP in economies with underdeveloped financial markets. Our model predicts that the aggregate TFP of the country with the least financial development will be almost 40 per cent below the US level.

The impact of financial frictions is particularly large in the large-scale, manufacturing sector. While the sector-level TFP declines by less than 30 per cent in services, it declines by more than 50 per cent in manufacturing, a result broadly in line with the available sector-level productivity data on 18 OECD countries. The differential impacts of financial frictions on sector-level productivity are reflected on the higher relative prices of manufactured goods to services in financially underdeveloped economies. The model accounts for a quarter of the observed relationship between the relative price and financial development.

Financial frictions also have a significant impact on the investment rate, when measured at common fixed prices across economies with different degrees of financial development. In our model simulations, the capital to output ratio (measured at common fixed prices)

declines by 15 per cent with financial frictions. Consistent with the data, this decline is almost entirely driven by the higher relative prices of manufactured investment goods in financially underdeveloped economies (Parente and Prescott, 2000; Hsieh and Klenow, 2007): the investment rates measured at respective equilibrium prices are roughly constant across economies with varying degrees of financial development.

Our quantitative analysis provides a clear decomposition of the main margins distorted by financial frictions. First, for a given set of heterogeneous production units in operation, financial frictions distort the allocation of capital among them (misallocation of capital). Second, for a given number of production units in operation, financial frictions distort the selection into entrepreneurship, with productive-but-poor individuals delaying their entry and incompetent-but-rich entrepreneurs remaining in business (misallocation of talent). Third, financial frictions distort the number of production units for a given distribution of entrepreneurial productivity in an economy. In our simulations, whereas the misallocation of capital is responsible for 90 per cent of the effect of financial frictions on the service sector TFP, it is the misallocation of talent that accounts for more than 50 per cent of the effect on the manufacturing sector TFP. The distortion on the number of entrepreneurs per se has negligible impacts on the productivity of either sector.

Finally, the differential impacts of financial frictions across sectors in our model produce an interesting testable implication on the establishment size distribution within each sector. Financial frictions, together with the resulting higher relative price of manufactured goods and lower capital rental rates and wages in the equilibrium, lead to too few entrepreneurs and too large establishments in the sector with large fixed costs, and too many entrepreneurs and too small establishments in the sector with small fixed costs. To evaluate this implication, we perform a detailed, disaggregate-level case study of Mexico and the US, and do find empirical support.

To emphasize the essence, our purpose is to provide a robust quantitative assessment of the role of financial markets in economic development. To this end, we incorporate into our framework elements of microeconomic heterogeneity and dynamics that enable a transparent mapping between our model and the data, which in turn disciplines our quantitative exercises. The two main elements are as follows: the establishment-level production technology has sector-specific non-convexities (fixed costs), with the resulting scale of operation larger in manufacturing (including the investment goods sector) than in services; and individuals are given the opportunities to overcome financial frictions over time with internal funds (self-financing).

**Empirical Underpinnings** Our theory is built on two premises: cross-country differences in financial development and cross-sector differences in the scale of establishments. Both of these underlying premises have strong empirical support.

The first premise, cross-country differences in financial development—underdevelopment in poor countries in particular, has been well established in the literature. King and Levine (1993a) and Beck et al. (2000) show that aggregate measures of credit and financial development are closely correlated with output per capita across countries, while La Porta et al. (1998) document that these macro indicators are strongly related to underlying institutional differences such as the enforcement of contracts, creditor protection, and so on. Banerjee and Duflo (2005) review the literature documenting micro-level evidence for credit constraints in poor countries and for the resulting misallocation of capital. In his detailed analysis of Thailand, Townsend (2010) links observed misallocation to micro-level credit constraints and shows how their relaxation through financial development leads to faster economic growth.

One empirical contribution of our paper is to establish the second premise: cross-sector differences in scale, defined as workers per establishment. Using detailed sector-level data from the OECD countries (the US in particular), we document that the average size of establishments varies substantially across broadly-defined sectors. For example, the average establishment in manufacturing is more than three times as large as that in services. This sectoral difference in establishment size is robustly observed in a wide range of countries.

In addition, we carry out a detailed case study of Mexico and the US to evaluate our model prediction on the impact of financial frictions on the establishment size distribution. We use data from the economic censuses of the two countries (based on the common, and hence comparable, North American Industrial Classification System) and a survey of small businesses in Mexico (which provides data on small-scale, mobile, and informal entrepreneurs). We examine the data at a more disaggregate level of industry classification than the manufacturing vs. services dichotomy. The average establishments in Mexico are substantially smaller, especially in the service industries. However, industries with large-scale establishments in the US (mostly in manufacturing) tend to have even larger establishments in Mexico.<sup>2</sup>

One could define and explore sectoral heterogeneity along other characteristics than scale, but few are as easily-measured, ubiquitous, or robust as scale. We present two sets of empirical findings that further support our decision to focus on scale. Firstly, scale seems to be closely related to productivity: using sector-level TFP data from a subset of OECD countries and price data from a broader cross-section of countries, we show that, even at a more disaggregate level of industry classification, poor countries are particularly

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<sup>2</sup>To the best of our knowledge, we are the first to document this pattern, which does conform to the conventional wisdom of a “missing middle” in less developed countries (Tybout, 2000).

unproductive and have higher relative prices in industries with larger scales. Secondly, in our model, financial frictions have differential impacts on sectors with different scales because our notion of scale (establishment size) translates directly into financing needs. The most widely-used empirical metric of financing needs is “external dependence” constructed by Rajan and Zingales (1998). We compute the external dependence for broadly-defined sectors in the US, and find that sectors with larger scales also have larger external dependence.

**Related Literature** This paper contributes to a vast literature relating financial frictions, entrepreneurship, and economic development, including theoretical contributions by Banerjee and Newman (1993), King and Levine (1993b), Aghion and Bolton (1997), Piketty (1997), and Lloyd-Ellis and Bernhardt (2000).

There have been relatively fewer quantitatively-oriented studies. Giné and Townsend (2004) and Jeong and Townsend (2007, 2008) have pioneered quantitative analysis of the link between financial frictions and development. They estimate models of the theoretical literature using data on Thailand’s growth experience. In a related vein, Buera and Shin (2008) study the transitional dynamics of economies with underdeveloped financial markets.

Amaral and Quintin (2009) and Greenwood et al. (2009) are recent contributions that quantify the long-run impact of financial frictions.<sup>3</sup> They study models that allow for sharp analytical characterizations of the equilibrium. In obtaining such tractability, they downplay the role of entrepreneurs’ self-financing.<sup>4</sup> In our model, entrepreneurs can partly overcome financial constraints over time with self-financing, and the presence of such an avenue seems to materially affect the quantitative results (Section 4.3). More important, we complement their work by building a multi-sector model with non-convex technologies at the establishment level. These features help better capture the aggregate impact of frictions, and generate richer disaggregate-level predictions that can be evaluated empirically.

This paper is more closely related and complementary to three others in the literature that emphasize the differential effects of financial frictions on different industries. Rajan and Zingales (1998), an empirical paper, creates an index of dependence on external sources of financing for various manufacturing industries and tests whether industries that are particularly dependent on financing grow relatively faster in countries with more developed financial markets. We reconstruct their measure of industry-specific financial dependence for our analysis, and show that our measure of sectoral scale (workers per establishment)

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<sup>3</sup>Erosa (2001) is an earlier contribution that abstracts from microeconomic heterogeneity. His analysis focuses on the wedge between deposit and lending rates.

<sup>4</sup>Caselli and Gennaioli (2005) focus on relatively low frequency dynastic shocks requiring the reallocation of capital from incompetent heirs to productive-but-poor entrepreneurs. They assume an exogenous saving rule, consequently disallowing endogenous saving and self-financing decisions.

is closely related to external dependence both in our model and in the data.<sup>5</sup> Erosa and Hidalgo Cabrillana (2008) is a theoretical paper showing how financial frictions can have differential effects on the productivity of manufacturing industries with different fixed cost requirements. We study a broader set of sectors, and quantify the impacts of financial frictions by introducing scale as an empirical measure related to fixed costs and financing needs. Castro et al. (2009) start from the premise that different sectors (consumption vs. investment goods) are characterized by different volatility of underlying idiosyncratic productivity shocks. They show that in economies with less risk-sharing, sectors with more volatile shocks (investment goods) are particularly unproductive. Methodologically, they use a tractable model to obtain insightful analytical characterizations. We view our approach as complementary to theirs. We focus on sectoral scale differences and cross-country differences in external financing—readily-measured and robust features in the data. Our model, with its rich dynamics and heterogeneity, eludes analytical tractability, but facilitates a clear mapping into data and a direct interpretation of the quantitative results.

Finally, we add to the broader literature on the role of micro-level distortions (Hopenhayn and Rogerson, 1993; Guner et al., 2008; Restuccia and Rogerson, 2008). Our results complement the empirical findings of Hsieh and Klenow (2009) in particular, who find a factor-of-two difference in manufacturing TFP due to the misallocation of capital and labor. We explicitly model one source of such misallocation (financial frictions), and include the service sector in our analysis. Furthermore, we explore how distortions affect the entry and exit decisions of establishments.

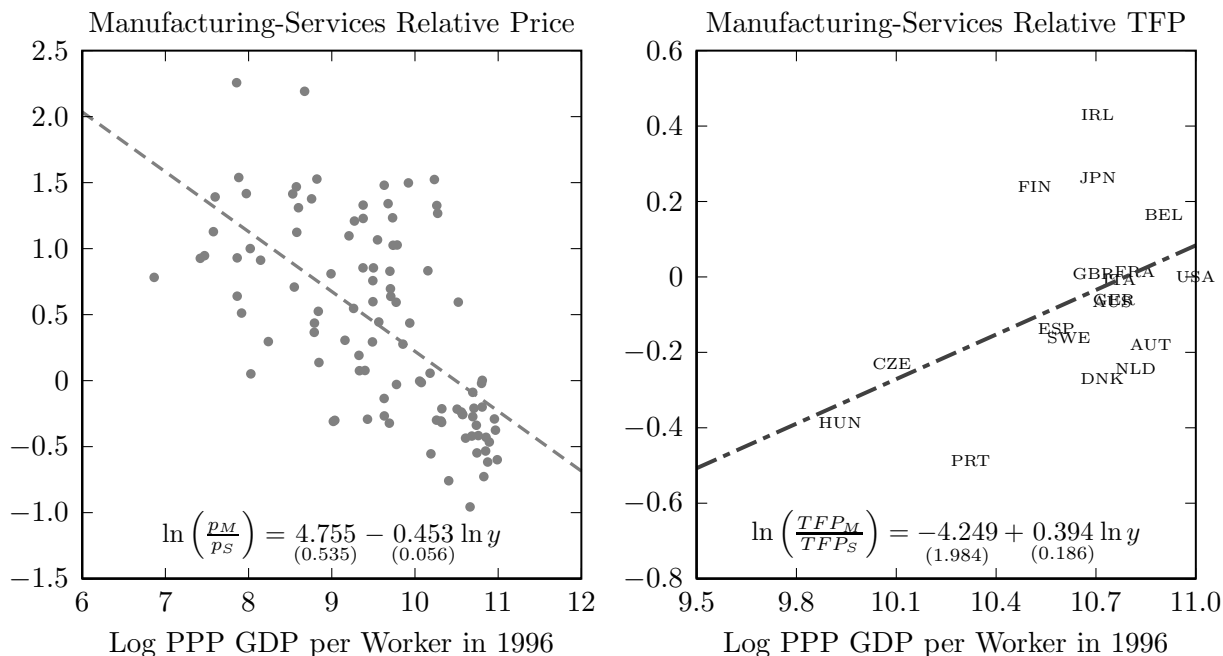
## 2 Facts

This section documents the key empirical facts motivating our study. First, we show that the price of manufactured goods is high relative to services in less developed countries, and that such relative prices are closely linked to sector-level relative productivity. Second, we point out that there are large differences in scale (establishment size) across sectors, with the manufacturing sector having much larger establishments on average than the service sector. Next, we emphasize this sectoral patterns in relative scale and relative productivity by showing that this relationship holds at a more disaggregate level as well: goods and services that are produced with large-scale technologies tend to be relatively more expensive in less developed economies, reflecting their low relative productivity in these industries.

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<sup>5</sup>Beck et al. (2008) examine the independent effects of scale and financing needs.

**Relative Prices, Relative Productivity, and Economic Development** In poor countries, the final prices of manufactured goods are high relative to services.<sup>6</sup> The left panel of Figure 1 shows this fact using the 1996 ICP benchmark by plotting the relative price of manufactured goods to services against PPP output per worker.<sup>7</sup> The log relative price of manufactured goods to services have a strong negative relationship with the log output per worker across countries. The slope coefficient of -0.45 is highly significant with a standard error of 0.06, and the regression has an  $R^2$  of 0.40.



**Fig. 1:** Relative prices (left panel) and relative productivity (right panel) against output per worker. In the left panel, the log relative price of manufactured goods to services is plotted against the log of PPP output per worker ( $y$ ) for each country. The price data are from the 1996 ICP benchmark, and the output data are from the Penn World Table 6.1. In the right panel, we construct sector-level TFP from the Productivity Level Database of the Groningen Growth and Development Centre. The log relative productivity of manufacturing to services is plotted against log output per worker. The standard errors of the regression coefficients are reported in parentheses.

<sup>6</sup>A related fact, first documented by Balassa (1964) and Samuelson (1964), is that the relative price of tradable goods is higher in poor countries.

<sup>7</sup>ICP stands for the International Comparison Programme of the United Nations. There are 115 ICP benchmark countries in 1996. To maintain a consistent sample, we present results based on the 102 countries for which Beck et al. (2000) constructed data on financial development. The results using all 115 countries are virtually identical. Here the relative price is compiled by creating Geary-Khamis aggregated prices for manufactured goods and services using 27 disaggregate product categories. The goods category consists of clothing, nine food and beverage categories, footwear, fuel, furniture/floor coverings, household appliances, household textiles/other household goods, machinery/equipment, tobacco, and transportation equipment. The services category consists of communication, education, medical/health, recreation/culture, rent/water, restaurants/hotels, and transportation services. We do not classify five final goods price categories: construction, changes in stocks, collective consumption by government, net foreign balance, and other goods and services.

Within many models, this relationship can be interpreted as lower relative TFP of manufacturing to services in less developed countries.<sup>8</sup> Indeed, in models with constant-returns-to-scale production functions and equal factor shares across sectors, relative prices equal the inverse of relative TFP (Hsieh and Klenow, 2007). Differences in factor shares and the relative supply of factors (e.g., higher levels of capital per worker) could break this inverse relationship, but empirically factor shares do not vary much across sectors (Valentinyi and Herrendorf, 2008).

Furthermore, the available data on sector-level productivity across countries support the relative productivity interpretation of relative prices. Using the Productivity Level Database (Inklaar and Timmer, 2008) of the Groningen Growth and Development Centre (GGDC), we construct sector-level TFP measures for manufacturing and services value-added for 18 OECD countries.<sup>9</sup> The log relative sector-level TFP of manufacturing to services is plotted against log GDP per worker in the right panel of Figure 1. The regression coefficient is 0.39. Given the smaller sample size, the standard error is larger (0.19), but the estimate is still significant at the five-percent level, with an  $R^2$  of 0.22. Thus, we find that the relative TFP of manufacturing to services is positively correlated with output per worker, just as relative prices are negatively correlated with output per worker, and the magnitudes are similar (0.39 and -0.45, respectively). This is comforting in two ways. Firstly, it confirms the predicted relationship between relative prices and relative productivity. Secondly, it gives evidence for value-added rather than final goods prices: we will explore these patterns in relative productivity, relative prices, and output per worker with a model that applies more transparently to value-added.

**Relative Prices and Financial Development** A common measure of a country’s level of financial development is its ratio of external financing to GDP, where external financing is defined as the sum of private credit, private bond market capitalization, and stock market capitalization.<sup>10</sup> As is well documented in the literature, this measure is very closely corre-

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<sup>8</sup>Alternative explanations include taxes, tariffs, and transportation costs that differ across sectors and countries.

<sup>9</sup>The database contains data for 19 of the 30 OECD countries (Australia, Austria, Belgium, Czech Republic, Denmark, Spain, Finland, France, Germany, Hungary, Ireland, Italy, Japan, Luxembourg, the Netherlands, Portugal, Sweden, the UK and the US) plus Slovenia. A double deflation method is used to construct real value-added by sector. While domestic intermediates are deflated by their source sector, imported intermediates are not. Imported intermediates are particularly important for two small countries with very high trade to GDP ratios, Luxembourg (112 per cent) and Slovenia (107 per cent). Trade to GDP ratios average 38 per cent for the remaining countries. These two countries are also strong outliers in terms of their sectoral TFP numbers (in opposite directions). We therefore exclude them in our analysis.

<sup>10</sup>We use the data from La Porta et al. (1998), Rajan and Zingales (1998), and Beck et al. (2000), which report the market value of stock market capitalization. We discount the reported stock market capitalization for two reasons. First, some equity (about three per cent in the US) is internally held by the

lated with output per worker: the regression of log GDP per worker on external financing to GDP yields a slope coefficient of 1.08, with a standard error of 0.13 and an  $R^2$  of 0.48. Therefore it is unsurprising that the relationship between log relative prices and external financing to GDP ratios is similar to the one between log relative prices and log GDP per worker in the left panel of Figure 1. The estimated slope coefficient is -0.67, with a standard error of 0.10 and an  $R^2$  of 0.38. For the 18 OECD countries with the sector-level TFP data, the regression coefficient of the log manufacturing-services relative TFP on external financing to GDP ratios is 0.08. While it has the same sign as the slope in the right panel of Figure 1, it is not significant with a standard error of 0.08.

The strength of the relationship suggests that financial development is potentially closely related to the patterns in relative prices, relative productivity, and output per worker across countries. In the model we develop, it is financial development that is the causal force behind these cross-country differences.

**Scale Differences across Sectors** Another key empirical fact that motivates our study is the clear differences in the scale of production units across broadly-defined sectors. Our interpretation is that the observed sectoral scale differences reflect differences in micro-level production technologies across these sectors. We will argue that these technological differences interact with financial development, so that financial development affects large-scale (e.g. manufacturing) and small-scale sectors (e.g. services) differently.

Here we use two measures of scale: workers per establishment and workers per enterprise. Establishments are locations of business, so that a single enterprise (i.e. firm) may have multiple establishments. Table 1 presents measures of average scale across broadly-defined final goods sectors in the US and other OECD countries, along with other sector-level characteristics like financial dependence and factor intensities.<sup>11</sup>

The first column is based on data from the 2002 US Economic Census, which uses an establishment basis and the NAICS classification. The second column is based on the OECD

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management (Clementi and Cooley, 2009). Second, the market value of equity overstates the book value which is conceptually closer to the financed capital investment in our model. Globally, the average of the book to market ratios is 0.45, while for the US it is 0.24. We choose to divide the reported stock market capitalization by three. Our cross-country regression results are robust to this correction, because the stock market is important for only a small number of countries (notably the US) in the data. We also note that some private credit is used for consumer credit (e.g. credit cards). In the US flow of funds data, this amounts to nine per cent of private credit during the 1990s. As we do not have data on consumer credit for most other countries—and this number is likely to be even smaller in those countries, we do not adjust for it.

<sup>11</sup>These sectors are constructed to be consistent with the final goods categories in the ICP data. Manufacturing consumption includes food/beverages, textiles, clothing, medicine, furniture, appliances, TVs and radios, cars, household items, and media. Equipment includes all manufactured equipment not included in consumption. Together, these two constitute manufacturing. Services include accommodation/food services, arts/entertainment, communication, education, FIRE, health, retail, sewage, transportation, and wholesale.

	Workers per Establishment	Workers per Enterprise	External Dependence	Capital Share
	US	OECD	US	US
Manufacturing	47	28	0.21	0.31
Services	14	8	0.09	0.27

**Table 1:** For the scale measures, we take simple averages in the US census data and the OECD SSIS data. The OECD data cover nine countries, and are complete at the enterprise level: Czech Republic, France, Germany, Hungary, Slovakia, Poland, Portugal, the UK, and the US. The external dependence ratio is calculated using the formula of Rajan and Zingales (1998), who measure the ratio of the difference between capital expenditures and cash flow to capital expenditures. Capital shares are from Valentinyi and Herrendorf (2008).

Structural Statistics for Industry and Services (SSIS) data for 2002. These data follow the common ISIC 3.2 four-digit classification, enabling comparison across OECD countries. Enterprise-level data permit comparison over the largest set of countries.<sup>12</sup>

Whether establishments or enterprises are the unit of measurement, the average scale varies considerably across sectors. In the US census data, establishments in manufacturing is on average 3.4 times as large as those in services (47 vs. 14). The relative scale of manufacturing to services is even larger with enterprises as the unit of observation. For the OECD average, the ratio is 3.5 (28 vs. 8). Establishments are our preferred unit of analysis because we think they embody production technologies, although we acknowledge that some technologies (e.g. the distribution system of Walmart) may be at the firm level. Data availability dictates which measure we use in certain cases.

In our model, financial frictions have differential impacts on sectors with different scales because our notion of scale (workers per establishment or enterprise) coincides with financing needs. Support for this interpretation can be obtained by comparing other measures of financing needs across sectors. The third column reports the measures of external dependence (Rajan and Zingales, 1998) that we construct using the US Compustat data for 1993–2003.<sup>13</sup> In the Compustat data, firms producing final manufacturing goods are substantially

<sup>12</sup>There are subtle differences in the definition of workers between the two samples. In particular, the SSIS data measure “number of persons engaged,” which can include some temporary or contract workers. The census data record “number of employees,” which excludes proprietors. For some countries, SSIS data have both measures, and the two mirror each other closely.

<sup>13</sup>Rajan and Zingales measure the ratio of the difference between capital expenditures (Compustat #128) and cash flow (Compustat #110, or the sum of #123, 125, 126, 106, 213, and 217, for format code 7) to capital expenditures. In order to negate the influence of outliers in noisy firm-level data, they take the total capital expenditures and total cash flow over the sample period to compute firm-specific numbers, and then pick the median value within an industry as the industry-specific value. Note that Rajan and Zingales only included the manufacturing sector in their study.

more financially-dependent than those producing services, with a median of 0.21 vs. 0.09.<sup>14</sup> While external dependence may be a more direct measure of financing needs or investment requirements, we decide to focus on scale (employment), a measure that is available for all firms in the economy, as opposed to just the publicly-traded firms in Compustat.<sup>15</sup>

Finally, the fourth column reports the sectoral differences in factor intensities. These numbers are from Valentinyi and Herrendorf (2008), and correspond to the capital share of gross output in each of these broadly-defined sectors, calculated using input-output data from the Industry Accounts of the Bureau of Economic Analysis. Unlike differences in scale and external dependence, the variation in factor intensity is relatively small.<sup>16</sup> We follow the recent literature (Chari et al., 1997; Hsieh and Klenow, 2007) and build a model that abstracts from these differences. Our focus is instead on the large observed differences in scale, and the corresponding financing needs, across sectors.

We note that the distinctions in Table 1 hold even at a more disaggregate level. Broadly-defined sub-sectors within manufacturing tend to have larger scales and higher dependence on external financing than services and construction, but all have comparable factor shares.<sup>17</sup>

**Relative Prices, Productivity, and Scale** We have established that the large-scale, manufacturing sector has higher relative prices and lower relative productivity in less developed economies. A natural question to ask is whether relative prices, relative productivity, and the scale of production technologies are related at a more disaggregate level as well.

We examine this issue using disaggregate ICP price data from its 1996 benchmark. The scale of an industry is constructed by averaging across eight countries for which comparable data are available.<sup>18</sup> We then map ICP categories into closely related groups of industries and calculate the average scale for these industry groups.<sup>19</sup> Finally, we run a cross-country

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<sup>14</sup>Alternative measures of firms' financing needs give a similar picture. For example, we have constructed a measure of setup costs. In particular, for each firm in Compustat, we have located the first period with positive excess investment, and calculated the average excess investment over following consecutive periods with positive excess investment. For the firms in manufacturing, the ratio of this measure over annual sales has a median of 0.65, while for those in services, the median is 0.12.

<sup>15</sup>See Davis et al. (2006) for an example where conclusions drawn from the universe of firms and from the set of publicly-traded firms are very different.

<sup>16</sup>Chari et al. (1997) also find little difference in factor shares between investment and consumption goods sectors, with, if anything, investment goods producers being more labor-intensive.

<sup>17</sup>See the earlier version of this paper, Buera et al. (2009).

<sup>18</sup>UNIDO SSIS data—which cover all industries, not just manufacturing—are available for eight countries (Czech Republic, France, Germany, Hungary, Poland, Portugal, Slovakia, and the UK), but only at the enterprise level. We therefore use number of persons engaged per enterprise as our measure of scale. For any given industry at a disaggregate level, there is a strong correlation in scale across countries. Still, we average across countries to smooth out idiosyncratic variations that may arise from local market structures, government regulations, and so on.

<sup>19</sup>A reliable mapping could not be done for four of the 29 ICP categories: other household goods, operation of transportation equipment, other goods and services, and collective consumption by the government. Also,

regression of 2,794 disaggregated ICP price data from 112 countries on log output per worker, log industry scale, and their interaction. The estimation result is (with standard errors in parentheses):

$$\ln \left( \frac{p_{i,j}}{PPP_i} \right) = \underset{(0.56)}{-7.48} + \underset{(0.05)}{0.29} \ln y_i + \underset{(0.15)}{1.01} \ln \bar{l}_j - \underset{(0.02)}{0.10} \ln y_i \ln \bar{l}_j, \quad R^2 = 0.22,$$

where  $p_{i,j}$  is the 1996 PPP price of industry  $j$  output in country  $i$ ,  $PPP_i$  is the average (Geary-Khamis) 1996 PPP price level in country  $i$ ,  $y_i$  is the output per worker of country  $i$  in 1996 international prices,  $\bar{l}_j$  is the average number of workers engaged per enterprise for industry  $j$ . The negative coefficient on the interaction term indicates that prices of the output of industries with larger scales are relatively higher in low income countries. Given the log difference between manufacturing and service scales in Table 1—i.e.,  $\ln(47/14) = 1.21$ , the coefficient of -0.10 implies a relative price elasticity with respect to output per worker of 0.12, about one-third of the full relationship in Figure 1.

We work out a parallel exercise using the disaggregate industry-level TFP data (29 industries) for the 18 OECD countries. We obtain a very similar result:

$$\ln \left( \frac{TFP_{i,j}}{TFP_i} \right) = \underset{(0.28)}{12.18} - \underset{(0.32)}{1.10} \ln y_i - \underset{(1.00)}{3.52} \ln \bar{l}_j + \underset{(0.09)}{0.32} \ln y_i \ln \bar{l}_j, \quad R^2 = 0.08.$$

The magnitude of the interaction term is substantially higher. With the difference between manufacturing and service scales in Table 1, the coefficient of 0.32 implies a relative TFP elasticity with respect to output per worker of 0.4, almost the full estimated elasticity between the two in the data (right panel, Figure 1).

The general magnitude and significance of these two regression results are quite robust. The significance of the results at the five-percent level are robust to clustering standard errors by country or by ICP category. Also, we can use  $p_{i,j}$  and  $TFP_{i,j}$  without scaling by  $PPP_i$  and  $TFP_i$  respectively. The results are nearly identical, except that the coefficient on  $\ln y_i$  is substantially larger in the relative price regression and smaller in the relative TFP regression. More generally, alternative specifications that use country-specific fixed effects instead of controlling for  $\ln y_i$  or category-specific fixed effects instead of controlling for  $\ln \bar{l}_j$  yield very similar results. Finally, substituting countries' ratios of external finance to GDP for  $\ln y_i$  produces again very similar coefficients for the relative price regression, and smaller but still significant coefficients (0.13) for the relative TFP regression.

We conclude that, even at a more disaggregate level, less developed countries have relatively high prices and low productivity in industries with larger scales. This is further evidence supporting our emphasis on sectoral scale differences.

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due to the lack of comparable data on agriculture, only the scale of food manufacturing establishments could be used. None of the food categories appears to be outliers.

### 3 Model

We model an economy with two sectors,  $S$  (small scale, services) and  $M$  (large scale, manufacturing). In each sector, there are two occupations: workers and entrepreneurs. The output of the service sector is used for consumption only. The manufactured goods are used for consumption and investment, and are the numeraire.

There are a measure  $N$  of infinitely-lived individuals, who are heterogeneous in their wealth and the quality of their entrepreneurial ideas or talent,  $z = (z_S, z_M)$ . Individuals' wealth is determined endogenously by forward-looking behavior. The vector of entrepreneurial ideas is drawn from a distribution  $\mu(z)$ . Entrepreneurial ideas “die” with a constant hazard rate of  $1 - \gamma$ , and a new vector of ideas is independently drawn from  $\mu(z)$ . The parameter  $\gamma$  therefore controls the persistence of the entrepreneurial idea or talent process.<sup>20</sup>

In each period, individuals choose their occupation: whether to work for a wage or to operate a business in sector  $S$  or  $M$ . Their occupational choices are based on their comparative advantage as an entrepreneur ( $z$ ) and their access to capital. Access to capital is limited by agents' wealth through an endogenous collateral constraint, because capital rental contracts may not be perfectly enforceable in our model.

One entrepreneur can operate only one production unit (establishment) in a given period. Entrepreneurial ideas are inalienable, and there is no market for managers or entrepreneurial talent. The way we model an establishment draws upon the span of control of Lucas (1978) and per-period fixed costs as in Rossi-Hansberg and Wright (2007).

**Preferences** Individual preferences are described by the following expected utility function over sequences of consumption  $c_t = (c_{S,t}, c_{M,t})$ :

$$U(c) = \mathbb{E} \left[ \sum_{t=0}^{\infty} \beta^t u(c_t) \right], \quad u(c_t) = \frac{1}{1-\sigma} \left( \psi c_{S,t}^{1-1/\varepsilon} + (1-\psi) c_{M,t}^{1-1/\varepsilon} \right)^{\frac{1-\sigma}{1-1/\varepsilon}}, \quad (1)$$

where  $\beta$  is the discount factor,  $\sigma$  the coefficient of relative risk aversion (and the reciprocal of the elasticity of intertemporal substitution),  $\varepsilon$  the intratemporal elasticity of substitution between services and manufactured goods, and  $\psi$  controls the share of services in overall consumption expenditure. The expectation is over the realizations of entrepreneurial ideas ( $z$ ), which depend on stochastic death of ideas ( $1 - \gamma$ ) and on draws from  $\mu(z)$ .

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<sup>20</sup>This shock can be interpreted as changes in market conditions that affect the profitability of individual skills.

**Technology** At the beginning of each period, an individual with vector of entrepreneurial ideas  $z$  and wealth  $a$  chooses whether to work for a wage  $w$  or operate a business in either sector  $j = S, M$ . To operate a business in a sector, individuals must pay a sector-specific per-period fixed cost of  $\kappa_j$ , in units of the sector's output. The crucial assumption is that the fixed cost to run an establishment in the manufacturing sector is higher than that in the service sector,  $\kappa_M > \kappa_S$ . This will generate the scale difference between the two sectors that we observe in the data. Note that  $\kappa_j$  is fixed costs that need to be paid in every period of operation. We discuss in Section 4.3 how the results will change if one were to introduce one-time fixed setup costs of starting a business.

After paying the fixed cost, an entrepreneur with talent  $z_j$  produces using capital ( $k$ ) and labor ( $l$ ) according to:

$$z_j f(k, l) = z_j k^\alpha l^\theta,$$

where  $\alpha$  and  $\theta$  are the elasticities of output with respect to capital and labor, and  $\alpha + \theta < 1$ , implying diminishing returns to scale in variable factors at the establishment level. Note that the factor elasticities are assumed to be the same in both sectors, consistent with the empirical findings in the literature (Chari et al., 1997; Valentinyi and Herrendorf, 2008).

Given factor prices  $w$  and  $R$  (rental rate of capital), the profit of an entrepreneur is:

$$\pi_j(k, l; R, w, p) = p_j z_j k^\alpha l^\theta - Rk - wl - (1 + r)p_j \kappa_j,$$

where  $r$  is the interest rate and  $p_j$  is the price of sector  $j$  output. Service sector output is only for consumption, and the manufacturing sector produces investment goods and manufactured consumption goods. We normalize  $p_M$  to one. For later use, we define the optimal level of capital and labor inputs when production is not subject to financial constraints:

$$(k_j^u(z_j), l_j^u(z_j)) = \arg \max_{k, l} \{p_j z_j k^\alpha l^\theta - Rk - wl\}.$$

The key feature of this technology is that the fixed costs introduce non-convexity. For any strictly positive fixed cost  $\kappa_j$ , the technology is feasible only if operated above the minimum scale; that is,  $z_j k^\alpha l^\theta \geq (1 + r)\kappa_j$ .<sup>21</sup>

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<sup>21</sup>The model can be extended to allow for a choice of technologies within each sector: a technology with a small fixed cost and low productivity,  $A_{1,j} z_j k^\alpha l^\theta - \kappa_1$ , and a technology with a large fixed cost and high productivity,  $A_{2,j} z_j k^\alpha l^\theta - \kappa_2$ , with  $A_{2,j} > A_{1,j}$  for  $j = S, M$  and  $\kappa_2 > \kappa_1$ . Note that in this extension fixed costs are technology-specific but not sector-specific. One can think of our current setup as a case where the productivity gains associated with the  $\kappa_2$ -technology is substantially larger for the manufacturing sector; that is,  $A_{2,M} \gg A_{2,S}$ .

**Credit and Rental Markets** Individuals have access to competitive financial intermediaries, who receive deposits, rent capital  $k$  at rate  $R$  to entrepreneurs, and lend entrepreneurs the fixed cost  $p_j \kappa_j$ . We restrict the analysis to the case where both borrowing and capital rental are within a period—that is, individuals’ financial wealth is non-negative ( $a \geq 0$ ). The zero-profit condition of the intermediaries implies  $R = r + \delta$ , where  $r$  is the deposit and lending rate and  $\delta$  is the depreciation rate.

Borrowing and capital rental by entrepreneurs are limited by imperfect enforceability of contracts. In particular, we assume that, after production has taken place, entrepreneurs have the option to renege on the contracts. In such cases, the entrepreneurs can keep a fraction  $(1 - \phi)$  of the undepreciated capital and the revenue net of labor payments:  $(1 - \phi) [p_j z_j f(k, l) - wl + (1 - \delta)k]$ . The only punishment is the garnishment of their financial assets deposited with the financial intermediary,  $a$ . In the following period, this entrepreneur in default will regain access to financial markets, and will not be treated any differently despite the history of default.

Note that  $\phi$  indexes the strength of an economy’s legal institutions enforcing contractual obligations. This one-dimensional parameter captures the extent of frictions in the financial market due to imperfect enforcement of credit and rental contracts. This parsimonious specification allows for a flexible modeling of limited commitment that spans economies with no credit ( $\phi = 0$ ) and those with perfect credit markets ( $\phi = 1$ ).

We consider equilibria where the borrowing and capital rental contracts are incentive-compatible and are hence fulfilled. In particular, we study equilibria where the rental of capital is quantity-restricted by an upper bound  $\bar{k}^j(a, z_j; \phi)$ , which is a sector-specific function of the individual state  $(a, z)$ . We choose the rental limits  $\bar{k}^j(a, z_j; \phi)$  to be the largest limits that are consistent with entrepreneurs choosing to abide by their credit contracts. Without loss of generality, we assume  $\bar{k}^j(a, z_j; \phi) \leq k_j^u(z)$ , where  $k_j^u$  is the profit-maximizing capital inputs in an unconstrained (static) problem in sector  $j$ .

The following proposition provides a simple characterization of the set of enforceable contracts and the rental limits  $\bar{k}^j(a, z_j; \phi)$  for  $j = S, M$ .

**Proposition 1** *Capital rental  $k$  in sector  $j$  by an entrepreneur with wealth  $a$  and talent  $z_j$  is enforceable if and only if*

$$\begin{aligned} & \max_l \{p_j z_j f(k, l) - wl\} - Rk - (1 + r)p_j \kappa_j + (1 + r)a \\ & \geq (1 - \phi) \left[ \max_l \{p_j z_j f(k, l) - wl\} + (1 - \delta)k \right]. \end{aligned} \quad (2)$$

*Therefore, the upper bound on capital rental that is consistent with entrepreneurs choosing to abide by their credit contracts can be represented with a function  $\bar{k}^j(a, z_j; \phi)$ , which is increasing in  $a$ ,  $z_j$  and  $\phi$ .*

Condition (2) states that an entrepreneur must end up with (weakly) more economic resources when he fulfills his credit and rental obligations (left-hand side) than when he defaults (right-hand side). This static condition is sufficient to characterize enforceable allocations because we assume that defaulting entrepreneurs regain access to financial markets in the following period.

This proposition also provides a convenient way to operationalize the enforceability constraint into a simple rental limit  $\bar{k}^j(a, z_j; \phi)$ .<sup>22</sup> As long as the unconstrained level of capital rental is not enforceable, the rental limit  $\bar{k}^j(a, z_j; \phi)$  is implicitly defined as the larger root of the equation given by the equality in condition (2). Rental limits increase with the wealth of entrepreneurs, because the punishment for defaulting (loss of collateral) is larger. Similarly, rental limits increase with the talent of an entrepreneur because defaulting entrepreneurs keep only a fraction  $1 - \phi$  of the output. In the rest of the paper, we restrict individuals' capital inputs to be less than or equal to the rental limit  $\bar{k}^j(a, z_j; \phi)$ .

While the enforceability of contracts as measured by  $\phi$  is not sector-specific, the equilibrium enforceable rental contracts, as captured by the rental limits  $\bar{k}^j(a, z_j; \phi)$ , do vary across sectors because of the differences in technology and output prices across sectors.

**Recursive Representation of Individuals' Problem** Here we discuss the problem solved by individuals. In particular, we define the value for an individual before the occupational choice,  $v(a, z)$ , as well as the value of being a worker,  $v^W(a, z)$ , and being an entrepreneur in sector  $j$ ,  $v^j(a, z)$ , for  $j = S, M$ .

Individuals maximize (1) by choosing sequences of consumption, financial wealth, occupations (including the sector), and capital/labor inputs if they choose to be entrepreneurs, subject to a sequence of period budget constraints and rental limits.

At the beginning of a period, an individual's state is summarized by his wealth  $a$  and the vector of abilities  $z$ . He then chooses whether to be a worker or to be an entrepreneur in sector  $S$  or  $M$  for the period. The value for him at this stage,  $v(a, z)$ , is the maximum over the value of being a worker,  $v^W(a, z)$ , and the value of being an entrepreneur in sector  $j$ ,  $v^j(a, z)$ , for  $j = S, M$ :

$$v(a, z) = \max \{v^W(a, z), v^S(a, z), v^M(a, z)\}. \quad (3)$$

Note that the value of being a worker,  $v^W(a, z)$ , depends on his assets  $a$ , and on his entrepreneurial ideas  $z$ , which may be implemented at a later date. Similarly, the value of

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<sup>22</sup>In general, the set of enforceable capital rentals dictated by (2) does not exactly correspond to  $k \leq \bar{k}^j(a, z_j; \phi)$ . For example, an entrepreneur who is only offered a very low (and unprofitable) level of capital will default if  $p_j \kappa_j$  is large enough,  $p_j \kappa_j > a$ . Notwithstanding this, the solution to the individual's problem subject to (2) coincides with the solution to the individual's problem subject to the simpler rental limit  $k \leq \bar{k}^j(a, z_j; \phi)$ . See the proof in the appendix.

being an entrepreneur in sector  $j$ ,  $v^j(a, z)$ , depends on the entire vector of entrepreneurial ideas, as he may switch sectors at a later date. We denote the policy function associated with the optimal occupation choice by  $o(a, z) \in \{W, S, M\}$ .

As a worker, an individual chooses a consumption bundle  $c = (c_S, c_M)$  and the next period's assets  $a'$  to maximize his continuation value subject to the period budget constraint:

$$\begin{aligned} v^W(a, z) &= \max_{c, a' \geq 0} u(c) + \beta \{ \gamma v(a', z) + (1 - \gamma) \mathbb{E}_{z'} [v(a', z')] \} \\ \text{s.t. } & p \cdot c + a' \leq w + (1 + r)a, \end{aligned} \quad (4)$$

where  $w$  is her labor income, and  $p$  denotes the vector of goods prices. The continuation value is a function of the end-of-period state  $(a', z')$ , where  $z' = z$  with probability  $\gamma$  and  $z' \sim \mu(z')$  with probability  $1 - \gamma$ . In the next period, he will face an occupational choice again, and the function  $v(a, z)$  appears in the continuation value.

Alternatively, individuals can choose to become an entrepreneur in sector  $j$ . The value function of being an entrepreneur in sector  $j$  is as follows.

$$\begin{aligned} v^j(a, z) &= \max_{c, a', k, l \geq 0} u(c) + \beta \{ \gamma v(a', z) + (1 - \gamma) \mathbb{E}_{z'} [v(a', z')] \} \\ \text{s.t. } & p \cdot c + a' \leq p_j z_j f(k, l) - Rk - wl - (1 + r)p_j \kappa_j + (1 + r)a \\ & k \leq \bar{k}^j(a, z_j; \phi) \end{aligned} \quad (5)$$

Note that an entrepreneur's income is given by period profit  $p_j z_j f(k, l) - Rk - wl$  net of fixed costs  $(1 + r)p_j \kappa_j$  plus the return to his initial wealth, and that his choices of capital inputs are constrained by the rental limit  $\bar{k}^j(a, z_j; \phi)$ .

**Stationary Competitive Equilibrium** A stationary competitive equilibrium is composed of: an invariant distribution of wealth and entrepreneurial ideas  $G(a, z)$ , with the marginal distribution of  $z$  denoted with  $\mu(z)$ ; occupation choice function  $o(a, z)$ , and policy functions  $c_S(a, z)$ ,  $c_M(a, z)$ ,  $a'(a, z)$ ,  $l(a, z)$ , and  $k(a, z)$ ; rental limits  $\bar{k}^j(a, z_j; \phi)$ ,  $j = S, M$ ; and prices  $w$ ,  $R$ ,  $r$ , and  $p$  such that:

1. Given  $\bar{k}^j(a, z_j; \phi)$ ,  $w$ ,  $R$ ,  $r$  and  $p$ , the individual policy functions  $o(a, z)$ ,  $c_S(a, z)$ ,  $c_M(a, z)$ ,  $a'(a, z)$ ,  $l(a, z)$ ,  $k(a, z)$  solve (3), (4) and (5);
2. Financial intermediaries make zero profit:  $R = r + \delta$ ;
3. Rental limits  $\bar{k}^j(a, z_j; \phi)$  are the most generous limits satisfying condition (2), with  $\bar{k}^j(a, z_j; \phi) \leq k_j^u(z_j)$ ;

4. Capital rental, labor, services, and manufactured goods markets clear:

$$\frac{K}{N} \equiv \int k(a, z) G(da, dz) = \int aG(da, dz) \quad (\text{Capital rental market})$$

$$\int l(a, z) G(da, dz) = \int_{\{o(a,z)=W\}} G(da, dz) \quad (\text{Labor market})$$

$$\int c_S(a, z) G(da, dz) = \int_{\{o(a,z)=S\}} \left[ zk(a, z)^\alpha l(a, z)^\theta - \kappa_S \right] G(da, dz) \quad (\text{Services market})$$

$$\int c_M(a, z) G(da, dz) + \delta \frac{K}{N} = \int_{\{o(a,z)=M\}} \left[ zk(a, z)^\alpha l(a, z)^\theta - \kappa_M \right] G(da, dz) \quad (\text{Manufactured goods market})$$

5. The joint distribution of wealth and entrepreneurial ideas is a fixed point of the equilibrium mapping:

$$G(a, z) = \gamma \int_{\{(\tilde{a}, \tilde{z}) | \tilde{z} \leq z, a'(\tilde{a}, \tilde{z}) \leq a\}} G(d\tilde{a}, d\tilde{z}) + (1 - \gamma) \mu(z) \int_{\{(\tilde{a}, \tilde{z}) | a'(\tilde{a}, \tilde{z}) \leq a\}} G(d\tilde{a}, d\tilde{z}).$$

**Perfect-Credit Benchmark** To clarify the basic mechanics of the model, we analyze the perfect credit benchmark,  $\phi = 1$ . This is an economy with unconstrained within-period borrowing and capital rental for production—that is,  $\bar{k}^j(a, z_j, \phi) = k_j^u(z_j)$  for all  $a$ —but without between-periods borrowing or consumption insurance. We present two results characterizing the production side of the perfect-credit economy under the assumption that entrepreneurial talents for the two sectors follow mutually independent Pareto distributions with the same tail parameter  $\eta$ ,  $(z_S, z_M) \sim \eta^2 (z_S z_M)^{-(\eta+1)}$  for  $z_j \geq 1$ ,  $j = S, M$ . This assumption permits approximate closed-form expressions for net sectoral production functions (sectoral output net of fixed costs), factor shares, and the establishment size distribution. In addition, it implies that the establishment size distribution within each sector exhibits a thick right tail, a salient feature of the data.<sup>23</sup> These characterizations will help us pin down the technological parameters of the model using the US data on establishment size distributions across and within sectors.<sup>24</sup>

<sup>23</sup>We cannot deviate too strongly from the assumption of mutual independence, or the tail in the service sector will become counterfactually much thinner than the tail in the manufacturing sector. In the extreme, if entrepreneurial ideas were perfectly correlated across sectors, the model would predict that even the smallest manufacturing establishment will have more employees than the largest service establishment.

<sup>24</sup>We solve the perfect-credit benchmark in two steps. First, given an aggregate supply of capital and the intratemporal (homothetic) consumption decisions, we solve for optimal production decisions, occupation choices, and prices. We then use the wage and entrepreneurial profits to solve for the saving decisions of individuals facing idiosyncratic shocks to entrepreneurial ideas. By aggregating over individuals, we obtain the aggregate supply of capital. A stationary equilibrium with perfect credit markets is a nested fixed point.

The first result is that the net output of a sector is given by a Cobb-Douglas, constant-returns-to-scale function of the population size ( $N$ ), sectoral capital inputs ( $K_j$ ) and labor inputs ( $L_j$ ).

**Proposition 2** *Assume that entrepreneurial talents for the two sectors follow mutually-independent Pareto distributions with the same tail parameter  $\eta$ ,  $(z_S, z_M) \sim \eta^2 (z_S z_M)^{-(\eta+1)}$  for  $z_j \geq 1$ ,  $j = S, M$ , and that active entrepreneurs are a small fraction of the population. Then the output of a sector, net of fixed costs, equals:*

$$Y_j(K_j, L_j; N) = A_j N^{\frac{1/\eta}{\alpha+\theta+1/\eta}} K_j^{\frac{\alpha}{\alpha+\theta+1/\eta}} L_j^{\frac{\theta}{\alpha+\theta+1/\eta}},$$

where

$$A_j = \frac{\left[ \frac{\eta(1-\alpha-\theta)}{\eta(1-\alpha-\theta)-1} \right]^{\frac{1}{1+\eta(\alpha+\theta)}} \left[ 1 - \frac{p_j \kappa_j}{p_j \kappa_j + w} \left( 1 - \alpha - \theta - \frac{1}{\eta} \right) \right]}{\left[ \frac{p_j \kappa_j + w}{p_j(1-\alpha-\theta)} \right]^{\frac{\eta(1-\alpha-\theta)-1}{1+\eta(\alpha+\theta)}}}.$$

In our calibration of the perfect-credit benchmark, active entrepreneurs are indeed a small fraction of the population (5.26 per cent), given the average of 18 employees per establishment in the US data. It follows that, as in the standard neoclassical sectoral growth model, the elasticities of output with respect to capital and labor are constant,  $\frac{\alpha}{\alpha+\theta+1/\eta}$  and  $\frac{\theta}{\alpha+\theta+1/\eta}$ , respectively. Unlike in the standard model, however, the elasticities are not equal to the factor shares, because entrepreneurs earn rents. In particular, payments to capital as a share of income equals:

$$s_{K,j} = \frac{RK_j}{Y_j(K_j, L_j; N)} = \frac{\alpha}{1 - \frac{p_j \kappa_j}{p_j \kappa_j + w} \left( 1 - \alpha - \theta - \frac{1}{\eta} \right)}.$$

For realistic parameterizations of the model,  $1 - \alpha - \theta - \frac{1}{\eta}$  is close to zero, and hence factor shares in the two sectors are approximately equal.<sup>25</sup>

Our second result pertains to the establishment size distribution in the perfect-credit benchmark. In particular, we show that the establishment size in each sector follows a Pareto distribution with tail coefficient  $\eta(1 - \alpha - \theta)$ , and that the overall establishment size distribution in the economy is a mixture of Pareto distributions. We also show that there is a direct mapping between the ratio of fixed costs to wage ( $p_j \kappa_j / w$ ) and the ratio between the average establishment sizes ( $\bar{l}_j$ ) of the two sectors.

**Proposition 3** *Assume that entrepreneurial talents for the two sectors follow mutually-independent Pareto distributions with the same tail parameter  $\eta$ ,  $(z_S, z_M) \sim \eta^2 (z_S z_M)^{-(\eta+1)}$*

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<sup>25</sup>One technical condition is  $1 - \alpha - \theta - \frac{1}{\eta} > 0$ . See the proof in the appendix.

for  $z_j \geq 1$ ,  $j = S, M$ , and that active entrepreneurs are a small fraction of the population. Then the establishment size distribution in each sector follows the power law:

$$\Pr [\tilde{l}_j > l] = \left( \frac{l(\hat{z}_j)}{l} \right)^{\eta(1-\alpha-\theta)}, \quad l \geq l(\hat{z}_j),$$

where  $l(\hat{z}_j)$  is the employment in the marginal establishment of sector  $j$ . Furthermore, the establishment size distribution in the aggregate economy is given by a mixture of Pareto distributions:

$$\Pr [\tilde{l} > l] = n_S \left( \frac{l(\hat{z}_S)}{l} \right)^{\eta(1-\alpha-\theta)} + n_M \left( \frac{l(\hat{z}_M)}{\max\{l, l(\hat{z}_M)\}} \right)^{\eta(1-\alpha-\theta)}, \quad l \geq l(\hat{z}_M),$$

where  $n_S$  and  $n_M$  are respectively the fraction of service and manufacturing establishments in the economy, with  $n_S + n_M = 1$ . Also, the ratio of the average establishment sizes of the two sectors is:

$$\frac{\bar{l}_j}{\bar{l}_{j'}} = \frac{p_j \kappa_j + w}{p_{j'} \kappa_{j'} + w}.$$

This last result suggests a simple way of identifying the relative magnitude of sector-specific fixed costs from their relative scale. In our model, the large scale of a sector arises from the large fixed costs at the establishment level.<sup>26</sup> In addition, the tail of the establishment size distribution identifies the parameter governing the distribution of entrepreneurial talents. In the next section, these observations will enable us to calibrate the model in a transparent manner. We then quantify the impact of financial frictions.

## 4 Quantitative Analysis

In this section, we first calibrate the perfect-credit benchmark of our model economy to the US economy. We then conduct experiments to assess the effect of financial frictions. In particular, we vary  $\phi$ , the parameter governing the degree of financial frictions, to obtain variations in external finance to GDP ratios that are comparable to the range observed in a cross-section of countries. We evaluate our model predictions for aggregate/sector-level TFP, output per worker, and capital to output ratios.

In our quantitative analysis we hold fixed all technological parameters across countries, and vary only the parameter governing financial frictions ( $\phi$ ). In particular, we assume that countries are endowed with the same entrepreneurial talent distribution. We maintain this

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<sup>26</sup>It is straightforward to show that the model analog of Rajan and Zingales's financial dependence measure increases with the fixed cost  $\kappa_j$  in the perfect credit benchmark: we average investment inclusive of fixed costs across entrepreneurs to construct our analog.

assumption because our goal is to isolate and quantify the direct impact of financial frictions. One of our main results is that, starting with the same potential pool of entrepreneurs, financial frictions distort the selection into active entrepreneurship. The productivity distribution of entrepreneurs in operation therefore differs across countries, with financial frictions lowering the mean and raising the dispersion of this distribution. The effect on the mean conforms to the conventional wisdom of aggregate TFP differences across countries. The increase in dispersion is consistent with the empirical findings of Hsieh and Klenow (2009), who show that less developed countries' establishment-level productivity (TFPQ in their terminology) dispersion is larger than that of the US. It would be straightforward to incorporate cross-country differences in the average productivity of potential entrepreneurs and workers by considering human capital and exogenous TFP differences. It is less obvious how one would discipline exogenous cross-country differences in higher moments of the entrepreneurial talent distribution.

## 4.1 Calibration

We calibrate preference and technology parameters so that the perfect-credit economy matches key aspects of the US, a relatively undistorted economy. In particular, our target moments include standard macroeconomic aggregates, features of the establishment size distribution within and across sectors, establishment dynamics, and the concentration of income in the population.

We need to specify values for eleven parameters: four technological parameters,  $\alpha$ ,  $\theta$ ,  $\kappa_S$ ,  $\kappa_M$ , and the depreciation rate  $\delta$ ; two parameters describing the process for entrepreneurial talent,  $\gamma$  and  $\eta$ ; the subjective discount factor  $\beta$ , the coefficient of relative risk aversion  $\sigma$ , the intratemporal elasticity of substitution  $\varepsilon$ , and the service share in consumption  $\psi$ .

Two preference parameters,  $\sigma$  and  $\varepsilon$ , and two technological parameters,  $\frac{\alpha}{1/\eta+\alpha+\theta}$  and  $\delta$ , can be set to standard values in the literature. We let  $\sigma = 1.5$  and  $\varepsilon = 1.0$ .<sup>27</sup> The one-year depreciation rate is set at  $\delta = 0.06$ , and we choose  $\frac{\alpha}{1/\eta+\alpha+\theta}$  to match the aggregate capital income share of 0.30.<sup>28</sup>

We are thus left with the seven parameters that are more specific to our study. We calibrate them to match seven relevant moments in the US data as shown in Table 2: the average size of establishments in services and in manufacturing; the employment share of

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<sup>27</sup>The estimate of Herrendorf et al. (2009) is close to one using data on final consumption of manufacturing and services. For value-added, Buera and Kaboski (2009) estimate the preference to be close to Leontieff: our choice of  $\varepsilon = 1.0$  (Cobb-Douglas) will thus understate the quantitative effects of financial frictions.

<sup>28</sup>We are being conservative in choosing a relatively low capital share: the larger the share of capital, the bigger the role of capital misallocation. This way, we are also accommodating the fact that some of the measured payments to capital are actually payments to entrepreneurial input.

Target Moments	US Data	Model	Parameter
Top 10% employment share	0.69	0.69	$\eta = 4.84$
Top 5% income share	0.30	0.30	$\alpha + \theta = 0.79$
Average scale in services	17	17	$\kappa_S = 0.00$
Average scale in manufacturing	47	47	$\kappa_M = 4.68$
Exit rate	0.10	0.10	$\gamma = 0.89$
Manufacturing Share of GDP	0.25	0.25	$\psi = 0.91$
Interest rate	0.04	0.04	$\beta = 0.92$

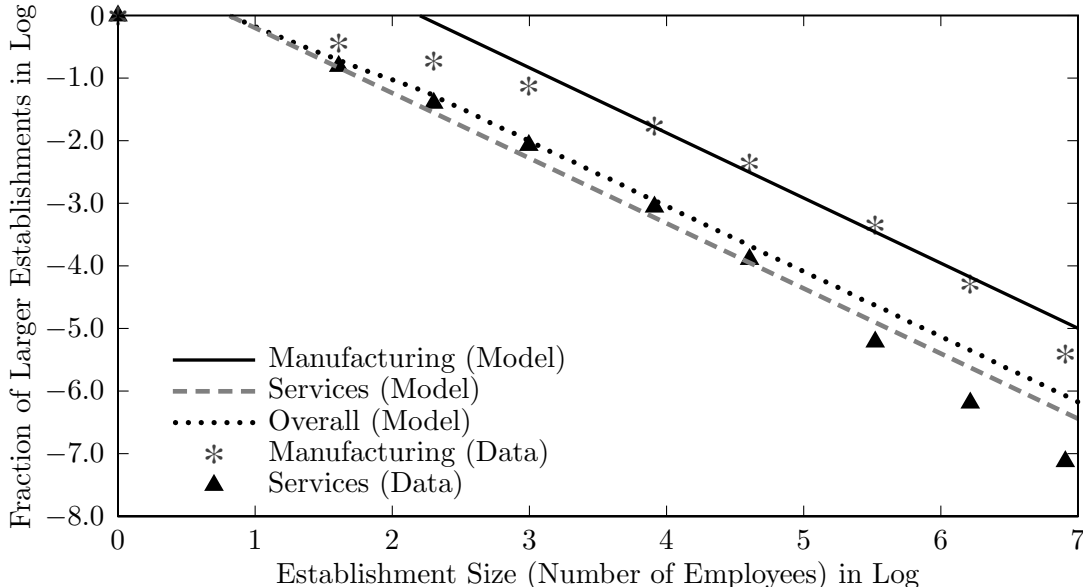
**Table 2:** Calibration

the top decile of establishments; the share of income generated by the top five percentile of earners; the annual exit rate of establishments; the share of manufacturing value-added in the absorbed GDP; and the annual real interest rate.

The identification of these seven parameters follows the basic logic given in our discussion of the perfect-credit benchmark. We calibrate the sector-specific fixed costs,  $\kappa_S = 0.0$  and  $\kappa_M = 4.68$ , to match the average establishment size in services and manufacturing (14 and 47, respectively). The per-period fixed cost in manufacturing sector,  $\kappa_M = 4.68$ , is tantamount to about three times the equilibrium wage in the perfect-credit benchmark. Given the returns to scale,  $\alpha + \theta$ , we choose the tail parameter of the entrepreneurial talent distribution,  $\eta = 4.84$ , to match the employment share of the largest ten percent of establishments, 0.63. We can then infer  $\alpha + \theta = 0.79$  from the income share of the top five percent of earners. Top earners are mostly entrepreneurs (both in the US data and in the model), and  $\alpha + \theta$  controls the fraction of output going to the entrepreneurial input. The parameter  $\gamma = 0.89$  leads to an annual establishment exit rate of ten per cent in the model. This is consistent with the exit rate of establishments reported in the US Census Business Dynamics Statistics.<sup>29</sup> We set  $\psi = 0.91$  to match the share of manufacturing value added in absorbed GDP. Note that all investment goods are manufactured goods in our model. Finally, the model requires a discount factor of  $\beta = 0.92$  to match the annual interest rate of four per cent.

Figure 2 shows the establishment size distribution from the calibrated perfect-credit benchmark (solid line for manufacturing, dashed line for services, dotted line for overall), and compares it with the US data (asterisk for manufacturing, triangle for services). The model is able to fit the tails of the empirical distribution, the distance between the two within-sector distributions, and the initial concavity in the overall (inclusive of both sectors) distribution of establishment size. The assumption that the entrepreneurial talents for the two sectors are drawn from the same Pareto distribution generates the identical slope for the right tails. The

<sup>29</sup>Note that  $1 - \gamma$  is larger than ten per cent, because a fraction of those hit by this idea shock will choose to remain in business. Entrepreneurs exit only if their new idea is below the equilibrium cutoff level in either sector.



**Fig. 2:** Establishment size distribution in the data and in the model. The horizontal axis is the establishment size (number of employees,  $l$ ) in log. For each  $l$ , we compute the fraction of establishments whose size is larger than or equal to  $l$ . This fraction in log is on the vertical axis. With our independent Pareto distribution for talent in each sector, the perfect-credit benchmark gives straight lines for services (dashed line) and manufacturing (solid line). We construct a line using all establishments in our perfect-credit benchmark (dotted line). We do the same calculation using the 2002 US Economic Census: asterisks for manufacturing and triangles for services.

model cannot capture the initial concavity in the distribution of establishment size within a sector, however, presumably because we are abstracting from within-sector heterogeneity in fixed costs.

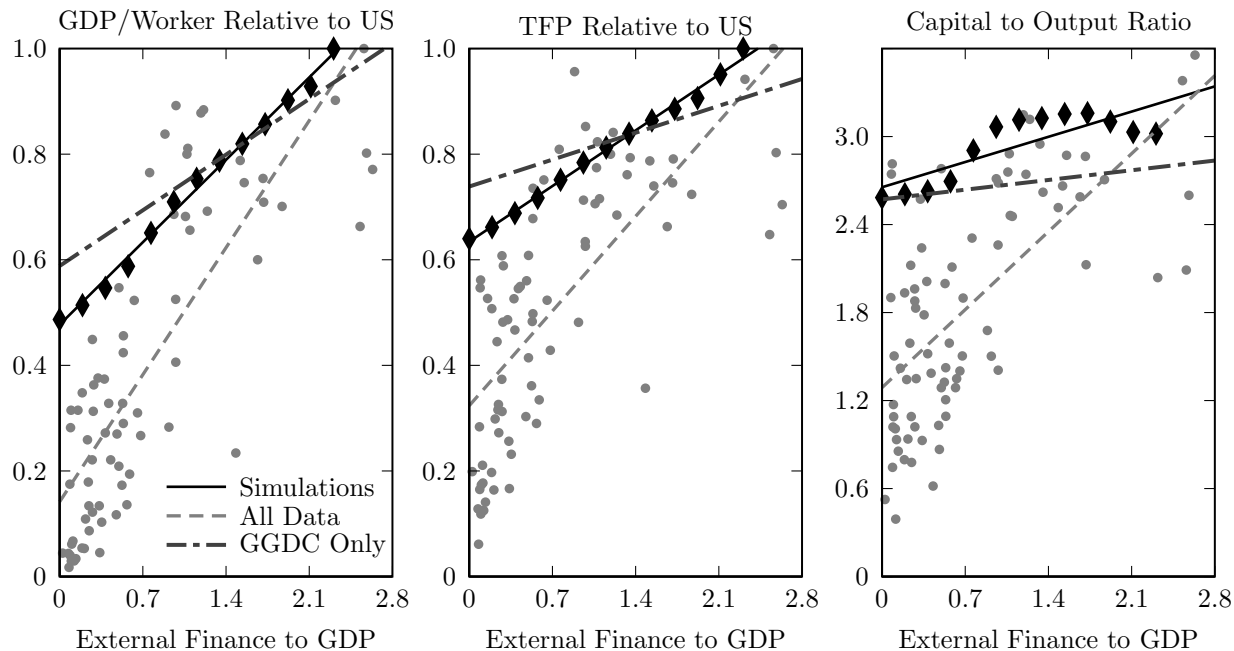
## 4.2 Results

In this section, we quantify the effect of financial frictions on economic development. We first show that financial frictions have a substantial, adverse impact on output per worker. In our exercises, the lower per-capita income in economies with financial frictions is primarily explained by their low aggregate TFP, with particularly low productivity in manufacturing. These results are consistent with the empirical findings in Section 2.

We vary  $\phi$ —the parameter governing the enforcement of contracts in condition (2)—to span a range of external finance to GDP ratios observed in the data. With quintiles of countries constructed in terms of GDP per worker at PPP, external finance to GDP ratios average 0.1 for the bottom quintile and 2.1 for the top quintile. The equilibrium external finance to GDP ratio is monotonically increasing in  $\phi$  in our exercises. We use 13 values of  $\phi$  ranging from 0 to 1, which span variations in external finance to GDP ratios from 0 to 2.3. The parameter  $\phi$  itself has no immediate empirical counterpart. Hence we plot the outcome

of our model simulations against the (endogenous) ratio of external finance to GDP implied by a given  $\phi$ .

The model quantities (e.g. output and TFP) are computed using a common fixed price, unless noted otherwise. In particular, we apply the output prices in the perfect-credit benchmark, with manufactured goods as numeraire. Similarly, the quantities in the data are measured at PPP.



**Fig. 3:** GDP per worker at PPP (left panel), aggregate TFP (center panel), and capital to output ratio at PPP (right panel) against the ratio of external finance to GDP. For GDP per worker and TFP, the country data are relative to the US and model simulations are relative to the perfect-credit benchmark. The solid lines are regression lines for model simulations ( $\blacklozenge$ ), and the dashed lines are for all countries ( $\bullet$ ). For a subset of OECD countries, data on non-agricultural output, TFP and capital stock are available. These individual data points are not shown, but the corresponding regression lines are plotted with dash-dot lines.

#### 4.2.1 Aggregate Impact of Financial Frictions

Figure 3 plots the effect of financial frictions on output per worker at PPP, aggregate TFP, and capital to output ratios. The diamonds are from model simulations, and the dots represent country-level data.<sup>30</sup> The solid lines are regression lines for the model simulations, and the dashed lines are for the country data.

<sup>30</sup>The data are from the PWT 6.1. We use a perpetual inventory method and a depreciation rate of six per cent to construct the capital stock, using only the 79 countries with investment data series starting in 1980 or earlier. TFP in 1996 is constructed as  $Y/(K^{1/3}L^{2/3})$ , where  $Y$  is PPP GDP and  $L$  is the number of workers.

In our model, the variation in financial frictions can bring down output per worker to less than half of the perfect-credit benchmark level (diamond, left panel). This is tantamount to the output per worker difference between countries like Malaysia and the US, or about 80 per cent of the US-Mexico difference. While this does not come close to the difference between the US and the poorest countries in sub-Saharan Africa, the magnitude is nevertheless sizable, considering that we are varying one single factor—financial markets—across countries. The regression coefficient of output per worker on external finance to GDP ratios is 0.22 for model simulations (solid line, left panel), and 0.34 for the data (dashed line, left panel).<sup>31</sup> Comparing the two coefficients, one may conclude that our model explains as causal two thirds of the cross-country relationship between output per worker and financial development.

As in the data, the per-capita income differences in our model are primarily accounted for by differences in TFP (Figure 3, center panel). Financial frictions can reduce aggregate TFP by 36 per cent in our model (diamond, center panel). The regression coefficient of aggregate TFP on external finance to GDP ratios is 0.15 for model simulations (solid line, center panel), and 0.26 for the data (dashed line, center panel).<sup>32</sup> Comparing the two coefficients, one can conclude that our model explains about 60 per cent of the cross-country relationship between aggregate TFP and financial development.

Another effect of financial frictions is the impediment of capital accumulation. The right panel of Figure 3 shows the relationship between capital to output ratio and external finance to GDP. In our model, the capital to output ratios fall by 15 per cent as we move from the perfect-credit benchmark to financial autarky (diamond), when measured at common fixed prices across economies. The regression coefficients of capital to output ratios on external finance to GDP are 0.25 for model simulations (solid line) and 0.76 for the data measured at international prices (dashed line). As we discuss below (Sections 4.2.2 and 4.2.3), financial frictions affect the manufacturing sector and the service sector differentially, with the result that manufactured investment goods become relatively more expensive than services. Consistent with the data (Hsieh and Klenow, 2007), this higher relative price of investment explains almost all of the fall in capital to output ratios: the saving and investment rates measured at respective equilibrium prices are roughly constant across our model economies with varying degrees of financial development. This is because of two opposing forces at work. Firstly, financial frictions lead to lower equilibrium interest rates and hence returns to saving, exerting downward pressure on aggregate saving. On the other hand, the resulting lower wages and capital rental rates increase the returns to self-financing for constrained entrepreneurs. These forces seem to offset, leaving the saving and investment

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<sup>31</sup>The univariate regression of output per worker on external finance in the data has an  $R^2$  of 0.64.

<sup>32</sup>The univariate regression of aggregate TFP on external finance in the data has an  $R^2$  of 0.51.

rates constant when measured at the respective equilibrium prices.

We also note that the factor-of-two difference in output per worker generated by our quantitative theory goes a long way if one were to focus on the factor-of-five difference in non-agricultural output per worker between the richest fifth percentile and the poorest fifth percentile of countries.<sup>33</sup> As we do not model the agricultural sector, ideally we would compare our model implications to data on non-agricultural output and productivity. The difficulty here is the dearth of data on sector-level capital stock that are comparable across countries.

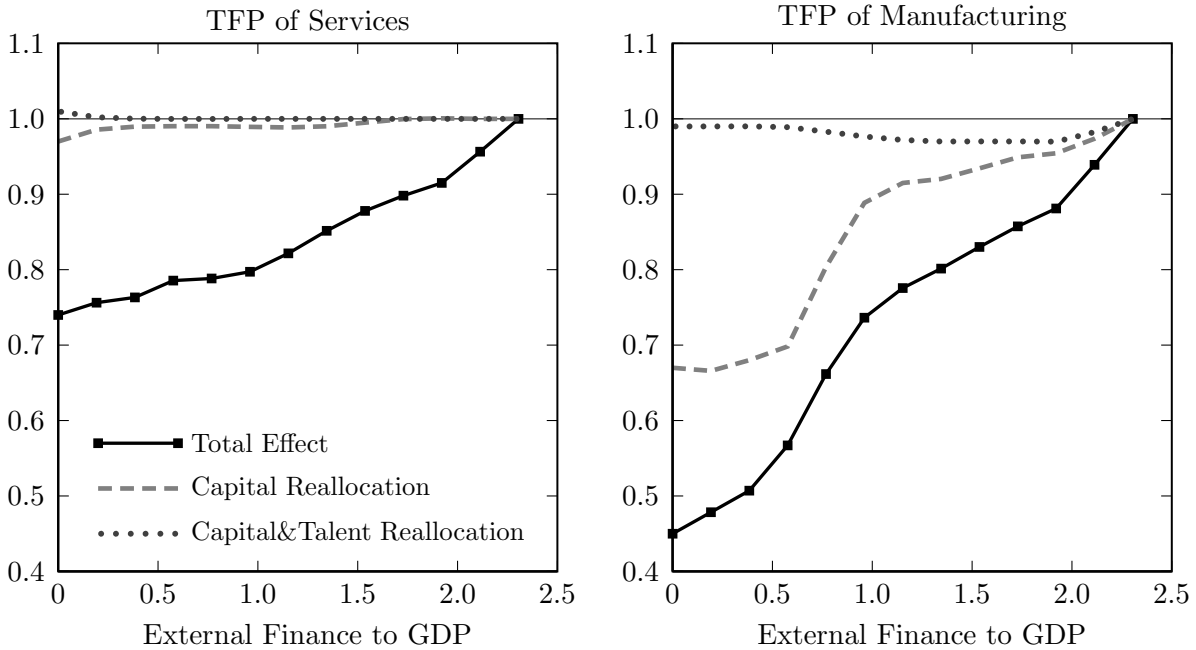
We address this issue in two ways. Firstly, we use the data set of Restuccia et al. (2008) covering 82 countries to run a univariate regression of non-agricultural output per worker on external finance to GDP ratios. The regression coefficient is 0.24, and the  $R^2$  is 0.45. This coefficient is about 30 per cent smaller than the one using the total output data (dashed line, left panel), and is very close to the slope, 0.22, generated by our model simulations (solid line, left panel): our model almost fully accounts for the empirical relationship between non-agricultural output per worker and financial development across countries. Secondly, because Restuccia et al. do not have data on capital input in the agricultural sector, we again turn to the Groningen Productivity Level Database and analyze the relationship between financial development and the performance of non-agricultural sectors.<sup>34</sup> In each of the three panels, we use a dash-dot line to show the regression line for these 18 OECD countries. We do not show individual data points. For these countries, the regression coefficients of non-agricultural output per worker, productivity, and capital to output ratios on financial development are smaller than those for the overall sample of countries. In fact, for this subset of countries, our model regression estimates in turn are quite comparable to the empirical relationships between the dependent variables and external finance to GDP. The regression coefficients on external finance to GDP are 0.15, 0.07, and 0.09, respectively for output per worker, TFP, and capital to output ratios (dash-dot lines). Recall that the corresponding regression coefficients are 0.22, 0.15, and 0.25 with our model simulations (solid lines).

In summary, financial frictions in our model can explain a large part of the cross-country differences in economic development, measured by output per worker, aggregate TFP, and capital to output ratios. If one were to focus on the non-agricultural sector, available data even more strongly support the quantitative results of our model.

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<sup>33</sup>See Restuccia et al. (2008) for a decomposition of cross-country per-capita income differences into agricultural and non-agricultural components.

<sup>34</sup>Among the 18 countries in the sample we use, Hungary is the poorest country, and also has the lowest external finance to GDP ratio (0.32). In the overall sample of the 79 countries analyzed here, Hungary ranks in the sixty-sixth percentile in terms of output per worker, and in the thirty-sixth percentile in terms of external finance to GDP.



**Fig. 4:** Decomposing the impact of financial frictions on sector-level TFP in services (left panel) and in manufacturing (right panel). Solid lines are the sector-level TFP in the simulated economies. TFP is normalized by its level in the perfect-credit benchmark, and plotted against the corresponding external finance to GDP ratio. Efficient reallocation of capital among existing active entrepreneurs raises TFP (dashed lines). When distortions on selection into entrepreneurship are undone as well, TFP further increases (dotted lines).

#### 4.2.2 Impact on Sector-Level Productivity

Financial frictions have differential impacts on the two sectors. The solid lines in Figure 4 trace the effect of financial frictions on the measured TFP of the service sector (left panel) and the manufacturing sector (right panel). While TFP declines by 25 per cent in services, the manufacturing sector TFP declines by 55 per cent with financial frictions. This result is consistent with the empirical observations that productivity differences across countries are sharpest for the large-scale, manufacturing sector (Section 2).

Next, we examine the driving forces behind these effects on sector-level productivity, which in turn determines the aggregate TFP. Intuitively, financial frictions distort the allocation of productive capital among entrepreneurs in operation. Those with binding collateral constraints will have a marginal product of capital higher than the rental rate. For instance, for the case of financial autarky, the standard deviation of log marginal product of capital equals 1.07 in services and 1.23 in manufacturing. In addition, financial frictions distort the entry and exit decisions of entrepreneurs: productive-but-poor entrepreneurs delay entry until they can overcome financing constraints, and incompetent-but-wealthy ones remain in business.

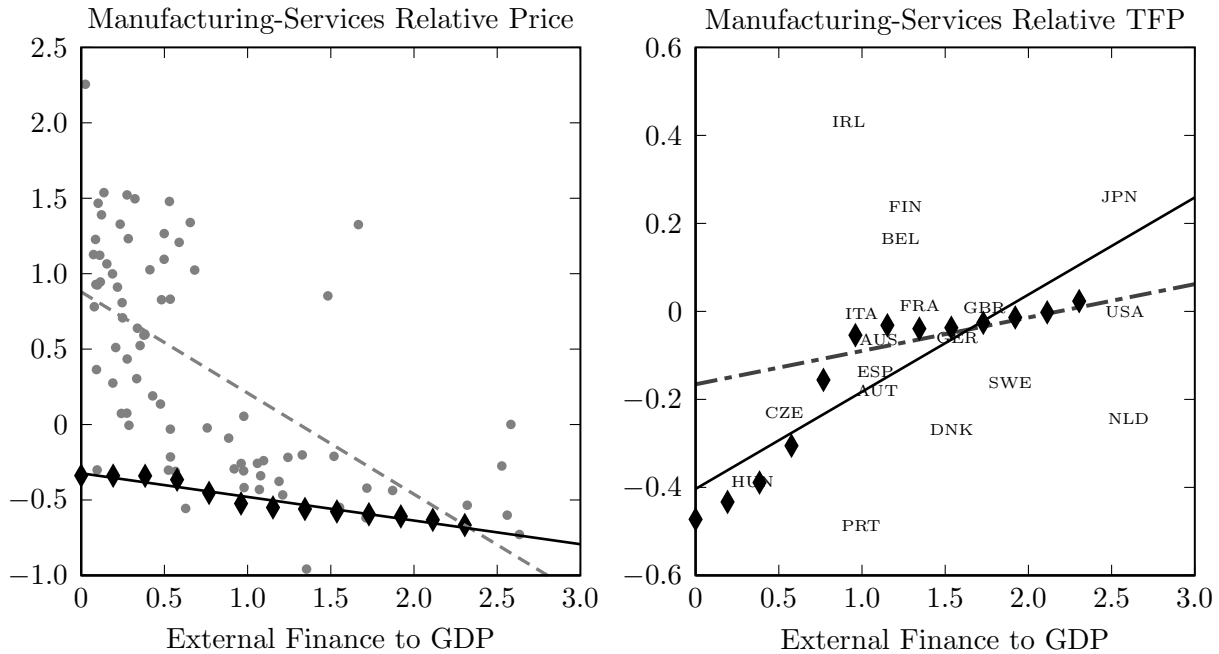
In Figure 4, we decompose the effects of financial frictions on sector-level TFP into

distortions on the allocation of capital across active entrepreneurs (intensive margin, or misallocation of capital), and into distortions on the allocation of entrepreneurial talent (extensive margin). The extensive margin is further decomposed into the number of active entrepreneurs in each sector, and into the distribution of talent among active entrepreneurs (misallocation of talent). To quantify this decomposition, we perform three experiments on our simulated economies. First, we reallocate capital among active entrepreneurs within each sector to equalize the marginal product of capital across them. For a given simulated economy, we hold fixed the number and the talent distribution of existing active entrepreneurs, as well as the total capital and labor employed in each sector. The sector-level TFP after this reallocation is the dashed lines in both panels. For the service sector, almost all of the low TFP is explained by the misallocation of capital among active entrepreneurs. For the manufacturing sector, this intensive-margin distortion explains less than half of the low TFP.

In the second experiment, while holding fixed the number of active entrepreneurs in each sector, we select the most talented individuals into entrepreneurship. We also allocate capital efficiently across the new set of active entrepreneurs, while holding constant the total capital and labor employed in each sector. The resulting sectoral TFP from this reallocation of talent and capital is the dotted lines. The misallocation of talent into entrepreneurship explains more than half of the low TFP in the large-scale, manufacturing sector, and less than one tenth of the low TFP in the small-scale, service sector.

Finally, in addition to the efficient reallocation of talent and capital above, we allow for the number of entrepreneurs to adjust in each sector at the perfect-credit equilibrium prices. This additional adjustment affects the TFP only slightly: The dotted lines from the second experiment are already close to the horizontal lines going through one, which represent the respective sector TFP levels in the perfect-credit benchmark. This last experiment suggests that restrictions to entry per se may not have significant quantitative effects unless the distribution of entrants is distorted.

The following conclusions can be drawn from these sector-level exercises. Because of their larger scale and financing needs, establishments in the manufacturing sector are more vulnerable to financial frictions. There is more misallocation of capital and entrepreneurial talent in manufacturing than in services. In particular, the distortions on the entry and exit decisions of entrepreneurs matter vastly more for manufacturing. This result suggests that modeling endogenous entry and exit is pivotal for capturing the full impact of financial frictions.

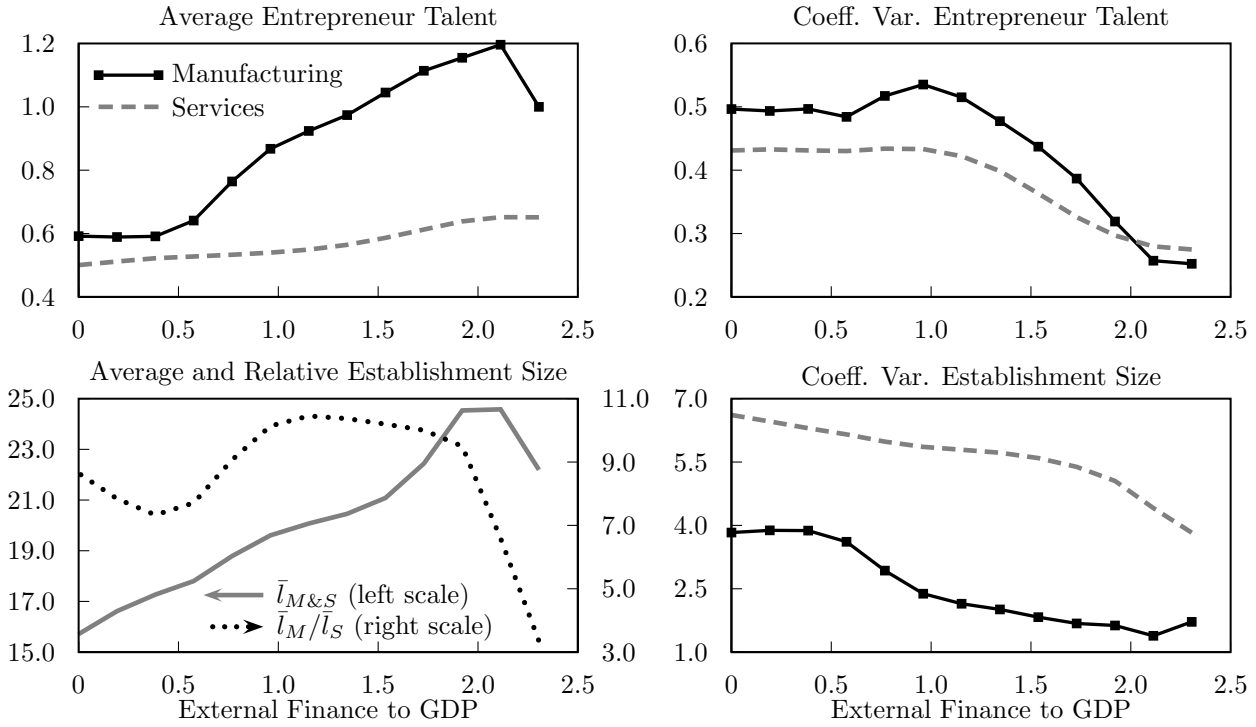


**Fig. 5:** Log relative price of manufacturing to services (left panel) and log relative productivity (right panel) against the ratio of external finance to GDP. Country data ( $\bullet$  in the left panel and three-letter codes in the right panel) and model simulations ( $\blacklozenge$ ). The price data are from the 1996 ICP benchmark, and the sector-level TFP are from the GGDC. The dashed and dash-dot lines are regression lines for the data, and the solid ones are for the model simulation.

### 4.2.3 Relative Productivity and Relative Prices

The pattern of relative productivity between the two sectors leads to the price of manufactured goods relative to services being higher in countries with underdeveloped financial markets. The left panel of Figure 5 plots the relative price of manufactured goods to services in log against external finance to GDP ratios. The regression coefficients are  $-0.67$  for the data (dashed line) and  $-0.16$  for model simulations (solid line): our model accounts for a quarter of the empirical cross-country relationship between the manufacturing-services relative price and financial development, leaving room for other explanations of relative prices that are correlated with financial frictions. As we have discussed in Section 4.2.1, this effect on relative prices helps explain the lower capital to output ratios observed in countries with less developed financial markets.

In the right panel of Figure 5, we plot the relative productivity of manufacturing to services in log against external finance to GDP ratios. The diamonds are the model simulations, with the corresponding regression line (solid line) that has a slope coefficient of  $0.22$ . We again turn to the Groningen database for the sector-level relative productivity in the 18 OECD countries (three-letter codes). The regression line (dash-dot line) has a slope coefficient of  $0.08$ : our model generates a relationship between relative sector-level productivity and financial development that is starker than the empirical one found in the available data.



**Fig. 6:** Impact of financial frictions on the distributions of establishment-level productivity and size. Clockwise from top left, all plotted against external finance to GDP ratios (horizontal axis): Average productivity ( $z_j$ ) of active entrepreneurs in services (dashed line) and in manufacturing (solid line), normalized by the average manufacturing entrepreneurial productivity in the perfect-credit benchmark; Coefficient of variation of the productivity of active entrepreneurs in each sector; Coefficient of variation of the establishment size (number of workers) in each sector; Average establishment size in the overall economy (solid gray line, left scale) and the ratio of average manufacturing establishment size to average service establishment size (dotted line, right scale).

#### 4.2.4 Impact on Distribution of Establishment-Level Productivity and Size

Financial frictions have impacts on the distribution of establishment-level productivity and size as well. The top left panel of Figure 6 plots the average talent or productivity ( $z_j$ ) of active entrepreneurs in manufacturing (solid line) and services (dashed line), normalized by the average manufacturing entrepreneurial productivity in the perfect-credit benchmark. With financial frictions, not only an individual's entrepreneurial talent but also his wealth determine whether he will be an entrepreneur or not in any given period. As a result, incompetent-but-wealthy entrepreneurs remain in business, and talented-but-poor individuals do not run businesses until they can self-finance the capital needed for a profitable scale. With more financial frictions (and hence less external financing in equilibrium), the selection into entrepreneurship gets more distorted, and the average talent of active entrepreneurs falls. Figure 4 has shown that such misallocation of talent is more rampant in the manufacturing sector, which is confirmed here: the average entrepreneurial talent in manufacturing

drops by 40 per cent with financial frictions, while it goes down by 20 per cent in services.<sup>35</sup>

With more financial frictions, an individual’s wealth has greater influence upon his decision of entry into and exit from entrepreneurship. As a result, individuals with more diverse entrepreneurial talents will be operating business in equilibrium: the within-sector distribution of establishment-level productivity ( $z_j$ ,  $j = S, M$ ) becomes more disperse, and its coefficient of variation increases (top right panel, Figure 6).

Next, we explore how financial frictions affect the establishment size distribution. In the bottom left panel of Figure 6, the solid line traces the average establishment size, inclusive of both sectors (left-hand side vertical axis). Financial frictions reduce the average establishment size by up to 30 per cent.<sup>36</sup> This is because lower equilibrium wages (and hence lower opportunity cost of entrepreneurship) lead more individuals, including those who are not particularly talented, to opt for entrepreneurship. In this sense, financial frictions generate too many establishments that are too small. This model prediction is consistent with available empirical evidence, although its magnitude is not as large (Tybout, 2000).

The marginal entrepreneurs in economies with financial frictions overwhelmingly choose to start businesses in the small-scale, service sector, where the establishment-level production technology commands less financing needs. The larger scale and financing needs in the manufacturing sector make it harder for entrepreneurs to start and grow there, reducing the number of manufacturing establishments in equilibrium. At the same time, the relative price of manufactured goods to services increases with financial frictions. As a result, the operating scale of manufacturing establishments relative to service establishments becomes even larger. The dotted line is the ratio of the average establishment size in manufacturing to that in services ( $\bar{l}_M/\bar{l}_S$ , right-hand side vertical axis). We further pursue this prediction in Section 4.2.5.<sup>37</sup>

For given output and factor prices, the size of an establishment (measured by the number of employees) is determined by the entrepreneurial talent and the collateral constraint: entrepreneurs with the same talent may operate at different scales, as they may have different

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<sup>35</sup>The average entrepreneurial talent in manufacturing is non-monotonic with respect to external finance to GDP. With moderate degrees of financial frictions, there seems to be a “positive” selection into entrepreneurship in manufacturing. This can be explained by the fact that high-talent entrepreneurs can overcome collateral constraints more easily than low-talent ones. First, for given output and factor prices, they make more profits, and so accumulate assets more quickly. Second, the credit limit  $\bar{k}(\cdot)$  is an increasing function of  $z$ . These forces seem to prevail when  $\phi$  is close to one. Also, in the right panel of Figure 4, the misallocation of talent margin does not explain much of the low manufacturing TFP over this region, even less than the number of entrepreneurs margin.

<sup>36</sup>The average establishment size first increases from 22.1 to 24.5, before it goes down to 15.4. The initial increase over the region where external finance to GDP is between 2.3 and 1.9 is the flip side of the fall in the number of establishments, especially in manufacturing.

<sup>37</sup>The model of Castro et al. (2009) has a similar prediction on the relative scale of sectors, with scale being measured in terms of capital per establishment.

levels of wealth (collateral). We have seen that financial frictions increase the dispersion of the talent distribution of active entrepreneurs, which is then compounded with the increased dispersion of the establishment size distribution for a given entrepreneurial talent (bottom right panel, Figure 6). As a result, the overall (inclusive of both sectors) establishment size distribution becomes more disperse with financial frictions, which is consistent with the “missing middle” in less developed economies (Tybout, 2000).

#### 4.2.5 Relative Scale of Sectors: A Case Study

One interesting model implication is that financial frictions lead to greater disparity in the average establishment size (scale) between the manufacturing and the service sectors. As discussed above, this result stems not only from the direct effect of financial frictions on entrepreneurial entry and exit decisions, but also from the general equilibrium effects on input and output prices.

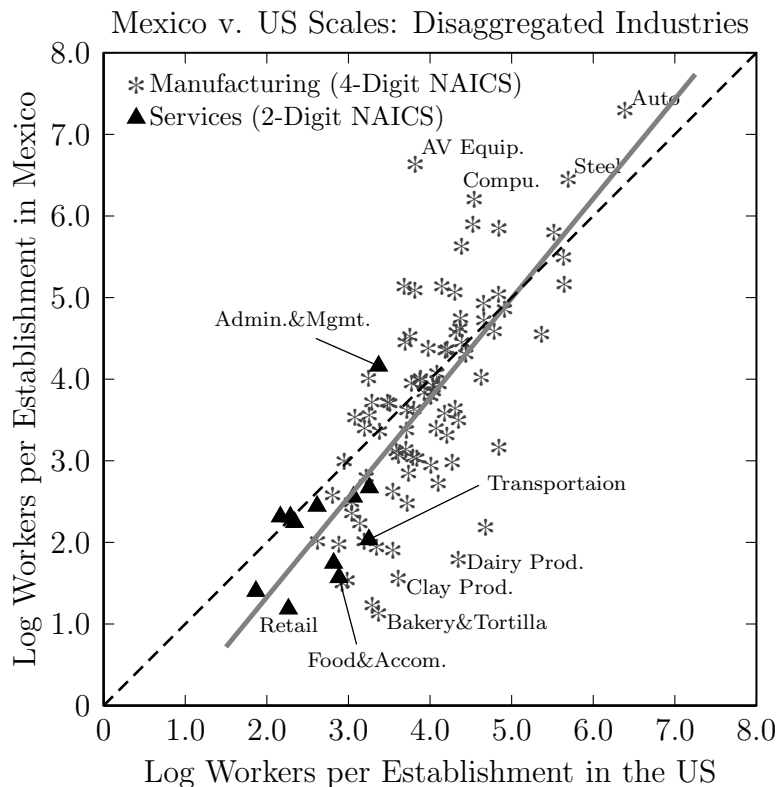
We evaluate this prediction using some new evidence from Mexico and the US. We compare establishment size data from the 2002 US Economic Census and the 2003 Mexican Economic Census, both of which follow the NAICS classification system and are hence directly comparable.<sup>38</sup> The two censuses have some substantial differences in their coverage. We use Mexico’s 1998 National Survey of Micro-Enterprises (ENAMIN) to impute corrections that make the US and the Mexican data fully comparable. These corrections include adjustments to remove non-employers—included in the Mexican Census but not for the US, and adjustments to add small-scale entrepreneurs without a fixed location—included in the US Census, though presumably unimportant, but not for Mexico, where they play an important role.

Figure 7 plots the average establishment size in Mexico (in log, vertical axis) against the average establishment size in the US (in log, horizontal axis) for 86 four-digit manufacturing industries and 12 two-digit service industries. The overall average establishment size is substantially smaller in Mexico than in the US, almost by a factor of three. However, many industries (those lying above the 45-degree line) have an average establishment that is larger in Mexico than in the US.<sup>39</sup> That is, the industries that are large scale in the US have an even larger scale in Mexico, while those that are small scale in the US have an even smaller scale in Mexico. With the exception of administration/management services, those above the 45-degree line are manufacturing industries. This finding supports our simulation results

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<sup>38</sup>For manufacturing, the classification schemes for Mexico and the US are identical, and allow for comparability at a very disaggregate level of industries (four digits). For services, however, the schemes differ and only allow for comparison at the two-digit industry level.

<sup>39</sup>Indeed, the data show a slope (solid line) that is significantly steeper than the 45-degree line (dashed line). The regression coefficient is 1.22 with a standard error of 0.11.



**Fig. 7:** Average establishment size of a given industry in Mexico (vertical axis) and in the US (horizontal axis): 86 industries in manufacturing and 12 in services. We use the data from the 2002 US Economic Census, the 2003 Mexican Economic Census, and Mexico’s 1998 National Survey of Micro-Enterprises. The solid line is the regression line, and the dashed line is the 45-degree line.

that the relative scale of manufacturing to services is larger with financial frictions.<sup>40</sup>

In addition, the fact that, at a more disaggregate industry level, Mexico has wider variations in scale than the US is consistent with our model prediction of more dispersed establishment size distribution in financially less developed economies.<sup>41</sup> A formal testing of this prediction, however, would require more detailed establishment-level data that are comparable across countries.

To summarize, using comparable establishment size data at a disaggregate industry level, we have shown that large-scale (mostly manufacturing) industries tend to have an even larger scale in Mexico than in the US, while small-scale industries have an even smaller scale in Mexico than in the US. This finding, hitherto undocumented in the literature, supports our

<sup>40</sup>There is other evidence consistent with our model prediction. Using the available OECD SSIS data, we find that financially less developed countries (Czech Republic, Hungary, Poland, Portugal, and Slovakia) have a larger relative scale of manufacturing to services (ranging from 3.4 to 4.1) than the US (3.1), where the sector-level scale is defined to be the number of workers per enterprise. The OECD SSIS data are designed for comparability across countries, but suffer from coverage issues.

<sup>41</sup>Erosa and Hidalgo Cabrillana (2008) report a related empirical fact: they show that the variance in output per worker across industries within the manufacturing sector is higher in poor countries.

model implication on relative scale of sectors. Furthermore, we also conjecture that our mechanism, in which scale differences lead to differential impacts of financial frictions across sectors, will also work at a more disaggregate level, not just at the level of the manufacturing vs. services dichotomy.

### 4.3 Discussions on Modeling Choices

We briefly discuss the robustness of our results to various modeling assumptions. We first consider other ways of generating scale differences between the two sectors, and then an alternative form of financing constraint. Finally, we compare some elements of our framework with other model specifications that have been conventional in the literature.

**Setup Costs** We have constructed numerical examples for a version of our model where the sectoral scale difference stems from one-time setup costs, rather than per-period fixed costs.<sup>42</sup> While these numerical examples are not precisely calibrated, we find that financial frictions have an even larger impact on aggregate and sector-level productivity, reflecting the stronger non-convexity that front-loaded setup costs impose. We choose our per-period fixed cost specification to avoid exaggerating the impact of financial frictions, especially when there are no reliable data on setup costs.<sup>43</sup>

**Span of Control Differences** We have also considered the possibility that the sectoral scale difference hinges on the establishment-level span of control. In particular, we set  $\alpha_j$  and  $\theta_j$ ,  $j = S, M$ , such that  $\alpha_S + \theta_S < \alpha_M + \theta_M$ , while the ratio  $\alpha_j/\theta_j$  is the same for  $j = S, M$ . The latter assumption reflects the empirical facts on factor shares reported in Table 1. In calibrated exercises with span-of-control differences and no fixed cost in either sector, we find that the effect of financial frictions is broadly consistent with our findings in Section 4.2, although the magnitude is not as large. One important distinction is the implication on the relative scale of the two sectors: with span-of-control differences, the relative scale of manufacturing to services decreases with financial frictions. Recall that our model with fixed cost differences predicts the opposite, consistent with our empirical findings in Section 4.2.5.

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<sup>42</sup>For the setup-cost version, we allow between-periods borrowing: that is,  $a$  can be negative. We assume that the debt of the entrepreneurs hit with idea shocks at the end of a period is forgiven. The lower bound on  $a$  is defined to be the most generous debt limit that is enforceable when the borrower is not hit with the idea shock. The zero-profit condition of the financial intermediary determines the spread between the deposit and borrowing rates.

<sup>43</sup>See, for example, Paulson and Townsend (2004) and McKenzie and Woodruff (2006) for discussions on setup and fixed costs for small establishments in developing countries. Sutton (1991) explains the difficulties of estimating setup costs using data from oligopolistic industries in developed countries.

**Simpler Collateral Constraint** We have also tried an alternative specification for the collateral constraint: a financing limit that does not depend on the entrepreneurial talent. More specifically, the sum of capital rental and fixed costs cannot exceed  $\lambda a$ , where  $\lambda$  is a parameter governing the degree of financial frictions and  $a$  is the financial wealth of an entrepreneur at the beginning of a period.<sup>44</sup> In calibrated exercises with this simpler constraint, the results are similar to those reported in Section 4.2, both qualitatively and quantitatively. One nice feature of this specification is that the average establishment size in the overall economy monotonically decreases with financial frictions, unlike the hump in the bottom left panel of Figure 6. We nevertheless go with a more general specification where collateral constraints depend endogenously on entrepreneurs' talent as well as wealth.

**Comparison with One-Sector Models** One immediate advantage of our two-sector model over one-sector models is its richer implications on relative prices, productivity, and scale between the two sectors. At the same time, our two-sector model generates a larger impact of financial frictions on aggregate output and productivity than a one-sector model, when both models follow the same calibration strategy in Section 4.1. For comparability, we choose the fixed cost  $\kappa$  in the one-sector model so that the ratios of total fixed costs to GDP are the same in the perfect-credit benchmarks of the two models. Recall from Section 4.2.1 that financial frictions can bring down aggregate output by 52 per cent, aggregate TFP by 36 per cent, and the capital to output ratio by 15 per cent. In the calibrated one-sector model, the effect is 39 per cent on output, 30 per cent on TFP, and virtually none on the capital to output ratio.<sup>45</sup>

In our calibration of the two-sector model, we have larger fixed costs for manufacturing establishments than for service establishments, and these fixed costs are disciplined by the scale differences between the two sectors.<sup>46</sup>

We conclude that the effect of the non-convexities (i.e. fixed costs) is itself convex: the aggregate impact of the large fixed costs borne by one part of the economy (manufacturing) is larger than that of the small fixed costs spread over the whole economy, holding constant the ratio of total fixed costs to GDP. In addition, there is a qualitative difference in the predictions on capital to output ratios between one-sector and two-sector models.

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<sup>44</sup>Here  $\lambda = 1$  corresponds to financial autarky where all capital needs to be self-financed, and  $\lambda \rightarrow \infty$  corresponds to the perfect-credit benchmark.

<sup>45</sup>In an alternative one-sector exercise, we assume that there is no fixed cost, while still following the same calibration strategy. The effect of financial frictions are even smaller without fixed costs: 35 per cent on output, 26 per cent on TFP, and again none on the capital to output ratio.

<sup>46</sup>We also discipline the relative importance of manufacturing vs. services in our economies using data on value-added GDP.

**Comparison with Two-Period Models: The Issue of Time Aggregation** Earlier attempts at quantifying the effect of financial frictions often relied on two-period overlapping-generation models. Given their tractability, two-period models are useful for qualitative characterizations of the economic mechanisms at work. However, there are difficulties in mapping these models into data and using them for quantitative purposes.<sup>47</sup> In particular, two-period models nearly preclude one important way of coping with financial frictions: self-financing. With the realistic time horizon in our model, a talented-but-poor individual saves up so that he can overcome the financial constraint over time and operate at the maximal-profit scale. In a two-period model, such a would-be entrepreneur is by construction condemned to the binding collateral constraint for half his life. As a result, the effect of financial frictions in a two-period model is made artificially larger. For example, in our own version of a two-period overlapping generation model, the aggregate effect of financial frictions is about 50 per cent larger than in our baseline model with more realistic time horizons, when both models follow the same calibration strategy as much as possible. Also, the lack of meaningful self-financing implies little growth in establishment size, and the average establishment size in equilibrium comes out artificially small.

## 5 Concluding Remarks

We have developed a quantitative theory linking financial development to output per worker, aggregate TFP, sector-level relative productivity, and relative prices. Financial frictions distort the allocation of capital and entrepreneurial talent, and have sizable adverse effects on a country's output per worker and aggregate productivity. Indeed, our model explains almost all of the cross-country relationship between output per worker or aggregate TFP and financial development, if one focuses on non-agricultural sectors. Establishments in sectors characterized by larger fixed costs operate most efficiently at larger scales, and hence have bigger financing needs. For this reason, they are more vulnerable to financial frictions than those in small-scale sectors. We have shown that this mechanism is quantitatively important, almost fully explaining the relationship between financial development and relative productivity of sectors in the available data. We have also shown that our mechanism is also consistent with the larger disparity in average establishment size across sectors observed in financially less developed countries.

Our theory and its quantitative implementation have revolved around the technological difference between two broadly-defined sectors: manufacturing vs. services. We have ab-

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<sup>47</sup>Amaral and Quintin (2009) provide a useful snapshot of the possible difficulties of doing quantitative work with two-period models, as well as some insights into how these challenges could be met.

stracted from the rich heterogeneity across industries within each sector, but our mechanism appears to play a role at a more disaggregate level as well. Such heterogeneity implies even larger differences in fixed costs or non-convexities across industries, and hence a more disaggregate model may lead to even larger effects of financial frictions on economic development.

Our analysis shows how micro-level (firm or establishment) technological differences across sectors interact with financial frictions and help us better understand such macroeconomic issues as aggregate productivity and sector-level relative productivity. In this context, we view the study of other micro-level distortions—e.g. size-dependent policies of Guner et al. (2008) or entry barriers of Djankov et al. (2002)—and their interaction with financial frictions as promising avenues for future research.

# Appendix

**Proof of Proposition 1** The rental of capital  $k$  in sector  $j$  is enforceable iff:

$$\tilde{v}^j(k; a, z) \geq v^d(a^d, z),$$

where  $\tilde{v}^j(k; a, z)$  is the value of a non-defaulting entrepreneur with wealth  $a$  and ability  $z$  that operates in sector  $j$  with rented capital  $k$ :

$$\begin{aligned} \tilde{v}^j(k; a, z) &= \max_{c, a'} \{u(c) + \beta[\gamma v(a', z) + (1 - \gamma) \mathbb{E}_{z'} v(a', z')]\} \\ \text{s.t. } pc + a' &\leq \max_l \{p_j z_j f(k, l) - wl\} - Rk - (1 + r) p_j \kappa_j + (1 + r) a. \end{aligned}$$

We define  $v^d(a^d, z)$  to be the value of a defaulting entrepreneur with ability  $z$  who gets to keep  $a^d = (1 - \phi) [\max_l \{p_j z_j f(k, l) - wl\} + (1 - \delta) k]$ :

$$\begin{aligned} v^d(a^d, z) &= \max_{c, a'} \{u(c) + \beta[\gamma v(a', z) + (1 - \gamma) \mathbb{E}_{z'} v(a', z')]\} \\ \text{s.t. } pc + a' &\leq (1 - \phi) \left[ \max_l \{p_j z_j f(k, l) - wl\} + (1 - \delta) k \right]. \end{aligned}$$

It is straightforward to see that  $\tilde{v}^j(k; a, z) \geq v^d(a^d, z)$  iff:

$$\begin{aligned} \max_l \{p_j z_j f(k, l) - wl\} - Rk - (1 + r) p_j \kappa_j + (1 + r) a \\ \geq (1 - \phi) \left[ \max_l \{p_j z_j f(k, l) - wl\} + (1 - \delta) k \right], \end{aligned}$$

which is equivalent to:

$$\begin{aligned} (1 + r) (a - p_j \kappa_j) &\geq ((1 - \delta) (1 - \phi) + r + \delta) k - \phi \max_l \{p_j z_j f(k, l) - wl\} \\ &= -\phi \left[ \max_l \{p_j z_j f(k, l) - wl\} - \frac{((1 - \delta) (1 - \phi) + r + \delta)}{\phi} k \right]. \end{aligned}$$

Notice that as long as  $f_{kk}(k, l) < 0$ ,  $f_{ll}(k, l) < 0$ ,  $\lim_{k \rightarrow 0} f_k(k, l) = \infty$  and  $\lim_{k \rightarrow \infty} f_k(k, l) = 0$ , the right hand side is minimized for some  $\hat{k}(z_j; \phi)$  such that  $0 < \hat{k}(z_j; \phi) < k_j^u(z_j)$ , as it equals  $-\phi$  times the profits of an entrepreneur facing a rental price  $((1 - \delta) (1 - \phi) + r + \delta) / \phi > r + \delta$ . The set of enforceable levels of capital rental can be easily characterized by a simple set of rental limits. There are two cases to consider.

If  $(1 + r) (a - p_j \kappa_j) > -\phi \left[ \max_l \{p_j z_j f(\hat{k}(z_j; \phi), l) - wl\} - \frac{((1 - \delta) (1 - \phi) + r + \delta)}{\phi} \hat{k}(z_j; \phi) \right]$ , there exists a unique function  $\bar{k}^j(a, z_j; \phi) \geq \hat{k}(z_j; \phi)$  given by the largest root of the equation:

$$(1 + r) (a - p_j \kappa_j) = (1 - \phi + r + \phi \delta) \bar{k}^j(a, z_j; \phi) - \phi \max_l \{p_j z_j f(\bar{k}^j(a, z_j; \phi), l) - wl\}.$$

Notice that if  $a - p_j \kappa_j < 0$ , there are two positive roots of the equation, with the smaller root satisfying  $\underline{k}^j(a, z_j; \phi) \leq \hat{k}(z_j; \phi)$ . In this case, the set of enforceable levels of capital rental is  $[\underline{k}^j(a, z_j; \phi), \bar{k}^j(a, z_j; \phi)]$ . If  $a - p_j \kappa_j \geq 0$ , the set of enforceable levels of capital rental is simply  $[0, \bar{k}^j(a, z_j; \phi)]$ . It is straightforward to see that  $\bar{k}^j(a, z_j; \phi)$  is strictly increasing in  $a$ ,  $z_j$ , and  $\phi$ .

If  $(1 + r) (a - p_j \kappa_j) \geq -\phi \left[ \max_l \{p_j z_j f(\hat{k}(z_j; \phi), l) - wl\} - \frac{((1 - \delta) (1 - \phi) + r + \delta)}{\phi} \hat{k}(z_j; \phi) \right]$ , we set  $\bar{k}^j(a, z_j; \phi) = 0$ . ■

**Proof of Proposition 2** In an economy with perfect credit markets, selection of individuals into entrepreneurship and sectors is determined by their entrepreneurial talents and relative prices. In particular, there exist two threshold ideas  $\hat{z}_j$ ,  $j = S, M$ , and a function  $\hat{z}_j(z_{-j})$ ,  $(j, -j) = (S, M), (M, S)$ , dividing the space of entrepreneurial ideas  $(z_S, z_M)$  into workers and entrepreneurs in the  $S$  and  $M$  sectors. These thresholds are defined by the following three indifference conditions:

$$(p_j \hat{z}_j)^{\frac{1}{1-\alpha-\theta}} \left(\frac{\alpha}{R}\right)^{\frac{1}{1-\alpha-\theta}} \left(\frac{\theta}{w}\right)^{\frac{\theta}{1-\alpha-\theta}} (1-\alpha-\theta) = w + p_j \kappa_j (1+r), \quad s = S, M, \quad (6)$$

$$\begin{aligned} (p_j \hat{z}_j (z_{-j}))^{\frac{1}{1-\alpha-\theta}} \left(\frac{\alpha}{R}\right)^{\frac{1}{1-\alpha-\theta}} \left(\frac{\theta}{w}\right)^{\frac{\theta}{1-\alpha-\theta}} (1-\alpha-\theta) - p_j \kappa_j (1+r) \\ = (p_{-j} z_{-j})^{\frac{1}{1-\alpha-\theta}} \left(\frac{\alpha}{R}\right)^{\frac{1}{1-\alpha-\theta}} \left(\frac{\theta}{w}\right)^{\frac{\theta}{1-\alpha-\theta}} (1-\alpha-\theta) - p_{-j} \kappa_{-j} (1+r). \end{aligned} \quad (7)$$

Integrating over individual output of entrepreneurs in sector  $j$  net of fixed costs, we obtain an expression for the net output of sector  $j$ ,

$$Y_j = N \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} z_j k(z)^\alpha l(z)^\theta \mu(dz) - \kappa_j (1+r) N \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} \mu(dz). \quad (8)$$

Using  $k(z) = \frac{z^{\frac{1}{1-\alpha-\theta}} K_j}{Z_j^{\frac{1}{1-\alpha-\theta}} N}$  and  $l(z) = \frac{z^{\frac{1}{1-\alpha-\theta}} L_j}{Z_j^{\frac{1}{1-\alpha-\theta}} N}$ , which follow from the first order conditions of the entrepreneurs' problem, we can rewrite (8) as:

$$\begin{aligned} Y_j &= N \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} z_j \left[ \frac{z_j^{\frac{1}{1-\alpha-\theta}} K_j}{Z_j^{\frac{1}{1-\alpha-\theta}} N} \right]^\alpha \left[ \frac{z_j^{\frac{1}{1-\alpha-\theta}} L_j}{Z_j^{\frac{1}{1-\alpha-\theta}} N} \right]^\theta \mu(dz) - \kappa_j (1+r) N \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} \mu(dz) \\ &= \frac{N^{1-\alpha-\theta} K_j^\alpha L_j^\theta}{Z_j^{\frac{\alpha+\theta}{1-\alpha-\theta}}} \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} z_j^{\frac{1}{1-\alpha-\theta}} \mu(dz) - \kappa_j (1+r) N \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} \mu(dz). \end{aligned}$$

Then,

$$Y_j = N^{1-\alpha-\theta} K_j^\alpha L_j^\theta Z_j - \kappa_j (1+r) N \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} \mu(dz), \quad (9)$$

where  $Z_j = \left[ \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} z_j^{\frac{1}{1-\alpha-\theta}} \mu(dz) \right]^{1-\alpha-\theta}$ .

Assuming  $\mu(dz) = \eta^2 (z_S z_L)^{-(\eta+1)}$  for  $z_j \geq 1$  and that entrepreneurs are a small fractions of the population—i.e.  $\hat{z}_j$  is large for  $j = S, M$ , we obtain

$$\begin{aligned} Z_j &= \left[ \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} z_j^{\frac{1}{1-\alpha-\theta}} \mu(dz) \right]^{1-\alpha-\theta} \approx \left[ \int_{\hat{z}_j}^{\infty} z_j^{\frac{1}{1-\alpha-\theta}} \eta z_j^{-(\eta+1)} dz_j \right]^{1-\alpha-\theta}, \\ \int_{\hat{z}_j}^{\infty} \int_1^{\hat{z}_j(z_j)} \mu(dz) &\approx \hat{z}_j^{-\eta}. \end{aligned}$$

Here, we further assume  $\frac{1}{\eta} < (1-\alpha-\theta)$  to guarantee that the integral is finite.

Using (6), as well as  $\frac{\alpha}{R} = \frac{K_j^{1-\alpha}}{L_j^\theta N^{1-\alpha-\theta}} \frac{1}{p_j Z_j}$  and  $\frac{\theta}{w} = \frac{L_j^{1-\theta}}{K_j^\alpha N^{1-\alpha-\theta}} \frac{1}{p_j Z_j}$ , we obtain

$$\hat{z}_j = \left\{ \frac{\left( \kappa_j (1+r) + \frac{w}{p_j} \right) \left[ \frac{(1-\alpha-\theta)}{\eta(1-\alpha-\theta)-1} \eta \right]^{\alpha+\theta}}{(1-\alpha-\theta) N^{-\alpha-\theta} K_j^\alpha L_j^\theta} \right\}^{\frac{1}{1+\eta(\alpha+\theta)}}. \quad (10)$$

Substituting into (9),

$$Y_j = A_j N^{\frac{1}{1+\eta(\alpha+\theta)}} K_j^{\frac{\alpha\eta}{1+\eta(\alpha+\theta)}} L_j^{\frac{\theta\eta}{1+\eta(\alpha+\theta)}},$$

where

$$A_j = \frac{\left[ \frac{\eta(1-\alpha-\theta)}{\eta(1-\alpha-\theta)-1} \right]^{\frac{1}{1+\eta(\alpha+\theta)}} \left[ 1 - \frac{p_j \kappa_j}{p_j \kappa_j + w} \left( 1 - \alpha - \theta - \frac{1}{\eta} \right) \right]}{\left[ \frac{p_j \kappa_j + w}{p_j(1-\alpha-\theta)} \right]^{\frac{\eta(1-\alpha-\theta)-1}{1+\eta(\alpha+\theta)}}}. \quad \blacksquare \quad (11)$$

**Proof of Proposition 3** From the first order condition of an entrepreneur of productivity  $z$  and that of the marginal entrepreneur ( $\hat{z}_j$ ), we obtain

$$l(z) = \left( \frac{z}{\hat{z}_j} \right)^{\frac{1}{1-\alpha-\theta}} l(\hat{z}_j).$$

Thus,

$$\Pr [\tilde{l}_j > l] = \Pr \left[ z > \left( \frac{l}{l(\hat{z}_j)} \right)^{1-\alpha-\theta} \hat{z}_j \mid z \geq \hat{z}_j \right] = \left( \frac{l(\hat{z}_j)}{l} \right)^{\eta(1-\alpha-\theta)}.$$

The aggregate establishment size distribution in the economy is then given by a mixture of Pareto distributions:

$$\Pr [\tilde{l}_j > l] = n_S \left( \frac{l(\hat{z}_S)}{l} \right)^{\eta(1-\alpha-\theta)} + n_M \left( \frac{l(\hat{z}_M)}{\max\{l, l(\hat{z}_M)\}} \right)^{\eta(1-\alpha-\theta)}, \quad l \geq l(\hat{z}_S).$$

Finally, by integrating  $l(z) = \frac{z^{1-\alpha-\theta}}{Z_j^{1-\alpha-\theta}} \frac{L_j}{N}$  over  $z$ , we calculate the average establishment size in sector  $j$ :

$$\bar{l}_j = \frac{L_j}{N(1-\mu(\hat{z}_j))}. \quad (12)$$

The optimal allocation of labor  $L_j$  and entrepreneurs  $N(1-\mu(\hat{z}_j))$  to sector  $j$  implies:

$$\theta p_j N^{1-\alpha-\theta} Z_j K_j^\alpha L_j^{\theta-1} = w, \quad (13)$$

$$(1-\alpha-\theta) p_j N^{-\alpha-\theta} Z_j K_j^\alpha L_j^\theta = p_j \kappa_j (1+r) (1-\mu(\hat{z}_j)) + w \mu(\hat{z}_j). \quad (14)$$

Taking the ratio of these two conditions, we obtain:

$$\frac{1-\alpha-\theta}{\theta} \frac{L_j}{N(1-\mu(\hat{z}_j))} = \frac{p_j \kappa_j (1+r)}{w} + \frac{\mu(\hat{z}_j)}{1-\mu(\hat{z}_j)}. \quad (15)$$

Substituting (14) into (10), we obtain:

$$\hat{z}_j = \left\{ \frac{\left( \kappa_j (1+r) + \frac{w}{p_j} \right) \left[ \frac{\eta(1-\alpha-\theta)}{\eta(1-\alpha-\theta)-1} \eta \right]^{\alpha+\theta}}{\frac{p_j \kappa_j (1+r) (1-\mu(\hat{z}_j)) + \frac{w}{p_j} \mu(\hat{z}_j)}{Z_j}} \right\}^{\frac{1}{1+\eta(\alpha+\theta)}}, \quad (16)$$

$$\frac{p_j \kappa_j (1+r)}{w} + \frac{\mu(\hat{z}_j)}{1-\mu(\hat{z}_j)} = \left[ \frac{p_j \kappa_j (1+r)}{w} + 1 \right] \frac{\eta(1-\alpha-\theta)}{\eta(1-\alpha-\theta)-1}. \quad (17)$$

Combining (12), (15) and (17), we obtain the desired expression:

$$\frac{\bar{l}_j}{\bar{l}_{j'}} = \frac{p_j \kappa_j + w}{p_{j'} \kappa_{j'} + w}. \quad \blacksquare \quad (18)$$

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